

3D Reconstruction

Simon Brenner

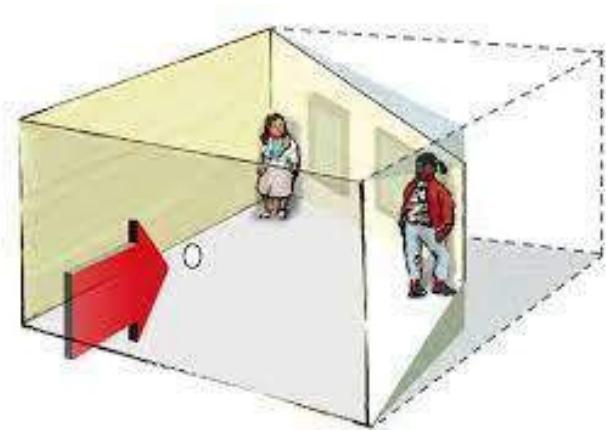
Digitale Transformation in der Handschriftenforschung – Computer Vision

Lecture Outline

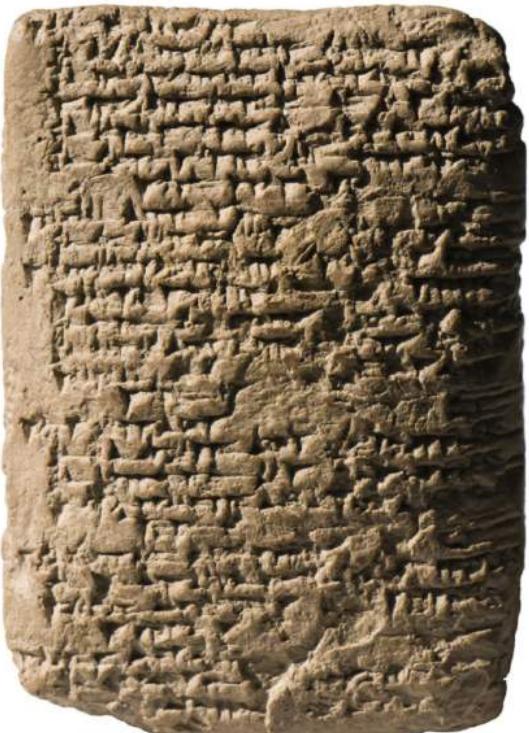
- **Introduction**
 - Why 3D reconstruction?
 - Basic concepts
- **Reconstruction Approaches**
 - Active triangulation
 - Range scanners
 - Photogrammetry (with how-to)
 - Photometric Stereo
- **Application to written heritage**
 - Examples from research

Introduction

- Photographs are 2D projections of a 3D world
- Result depends on
 - Angle of view
 - Focal length / distance
 - Lighting
- Sometimes we need to know the actual shapes of things
 - Documentation
 - Measurements (lengths, volumes)
 - Simulations
 - Animations / Games



3D written heritage – some examples



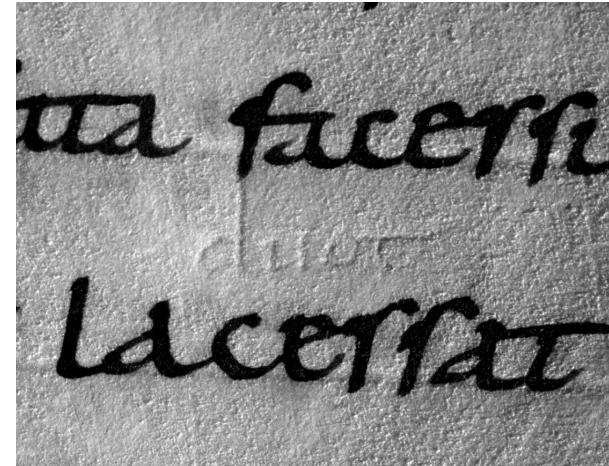
Cuneiform tablets



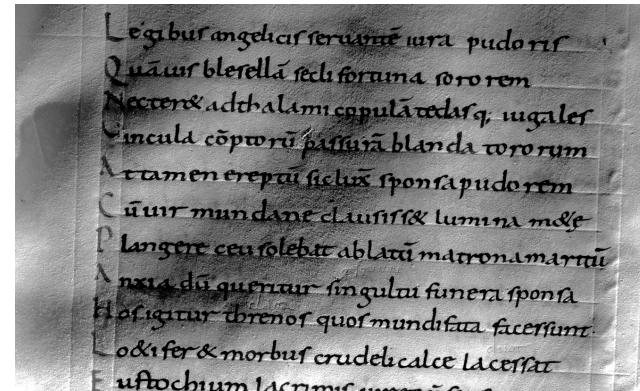
Etruscan bronze mirrors



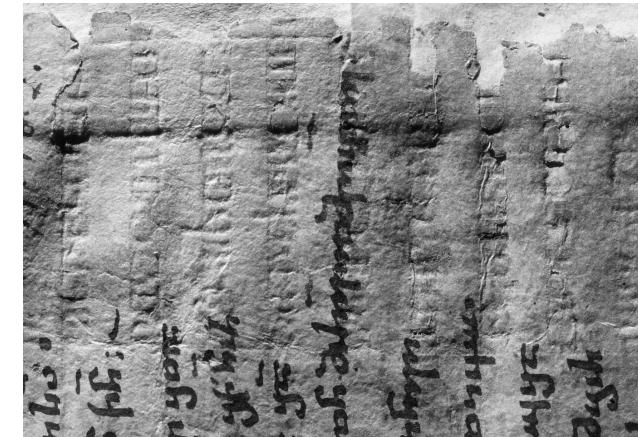
Coins



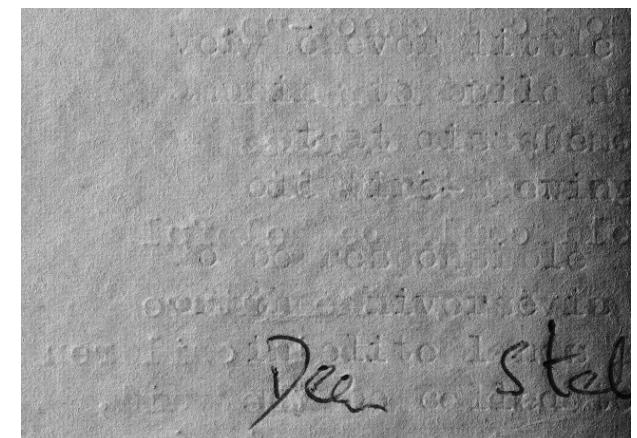
Dry-point glosses



Dry-point ruling



Ink corrosion

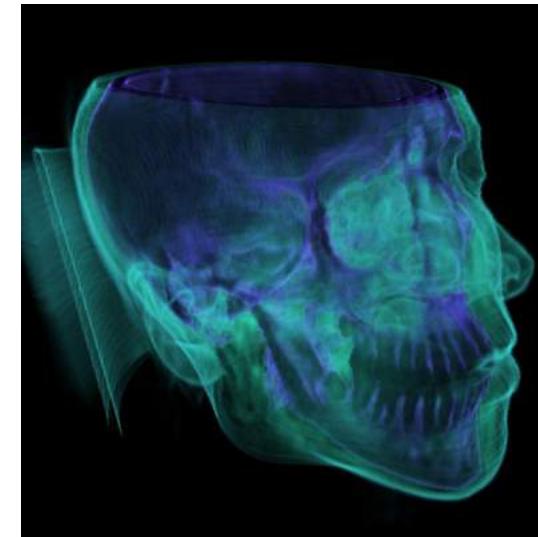
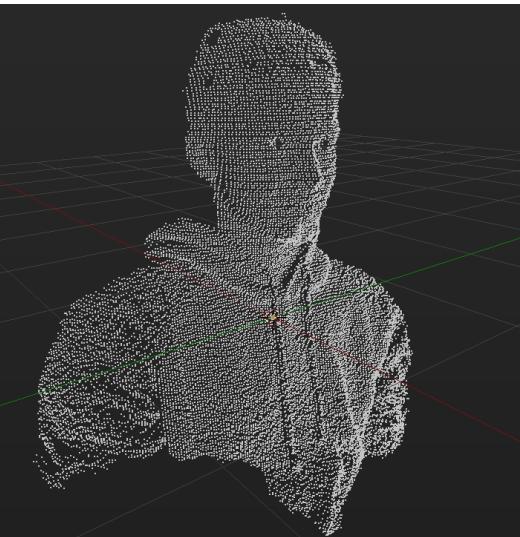
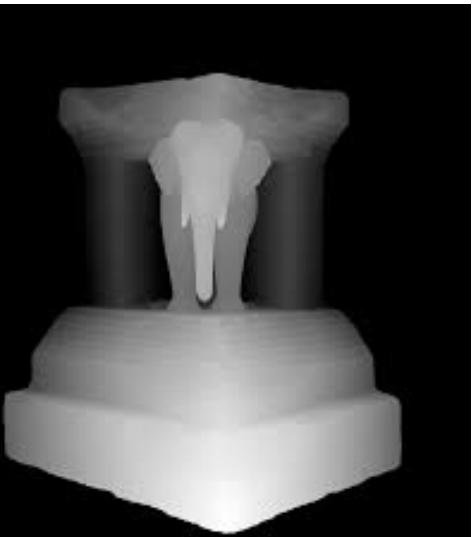


Typewriter indentations

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3D Representations



Depth map

- An image, where each pixel represents the distance to the observer
- Only one perspective
→ "2.5D"

Point cloud

- Collection of points with 3D coordinates (x,y,z)
- No neighborhood information
- Raw 3D scanning data often in this form

Surface model / mesh

- Vertices (points)
- Edges between vertices
- Faces between edges
- Very useful representation for visualizations, animations, games, etc.

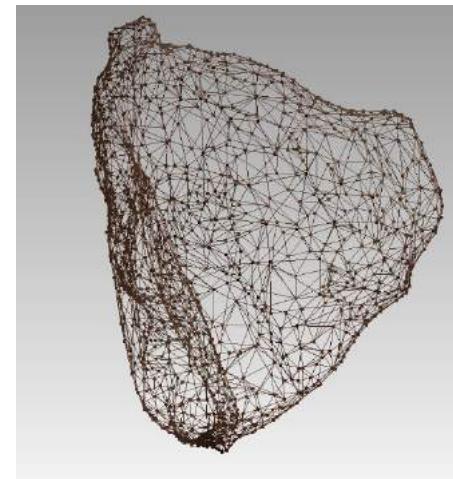
Volumetric data

- 3D space is partitioned into "Voxels", representing e.g. material density
- No explicit surfaces
- Produced by CT, MRI

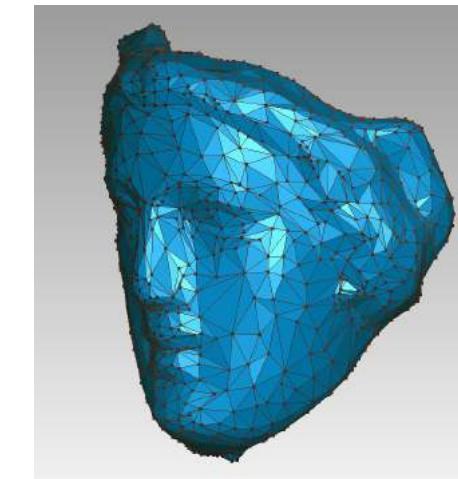
Surface model / mesh



vertices



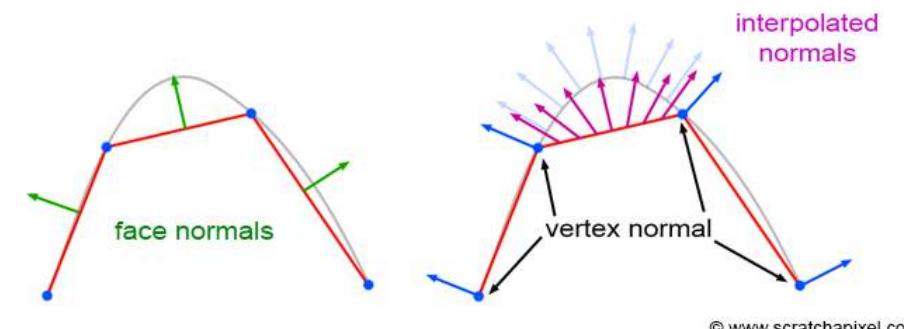
vertices + edges



vertices + edges +
faces = mesh

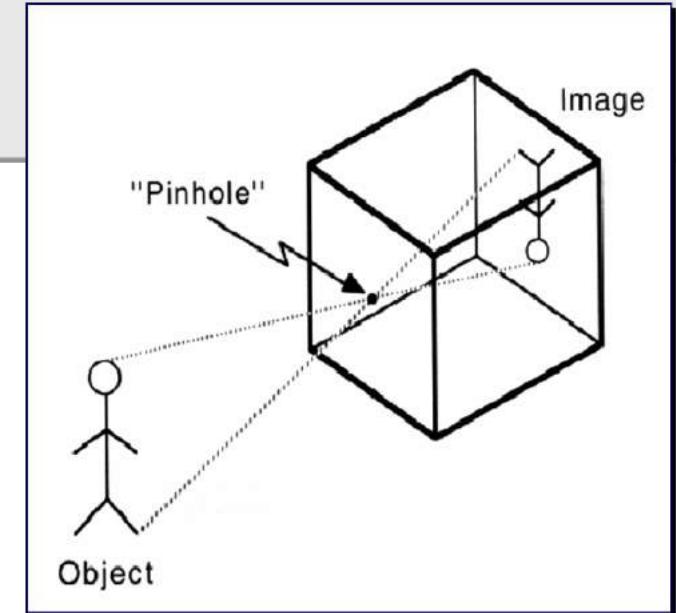
Surfaces are oriented (have a front and back side)

Normal vectors indicate the orientation (and are vital for rendering)



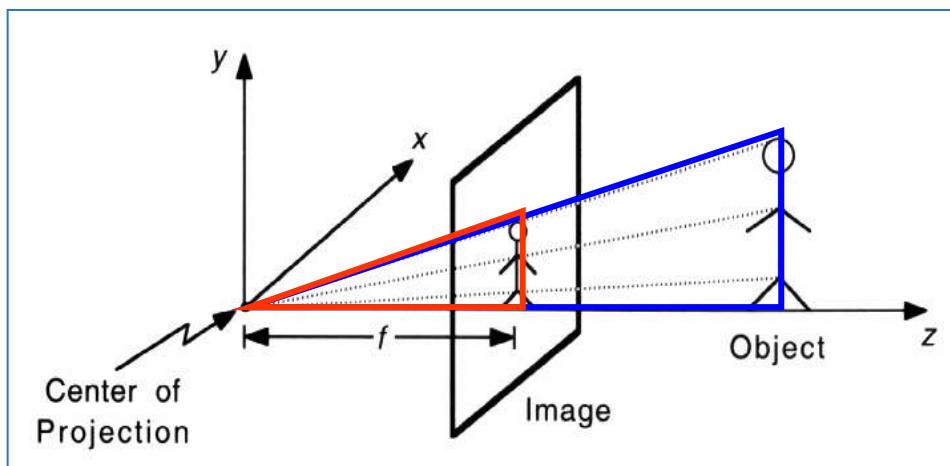
Pinhole camera model

- Simplified image formation model
- Reasonable approximation for many 3D vision applications



$$x = \frac{f}{Z} X$$

$$y = \frac{f}{Z} Y$$



$$\frac{x}{X} = \frac{f}{Z}$$

$$\frac{y}{Y} = \frac{f}{Z}$$

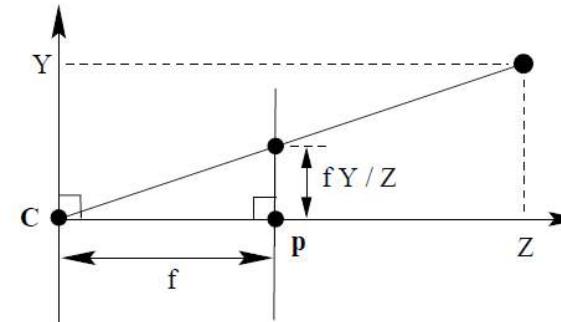
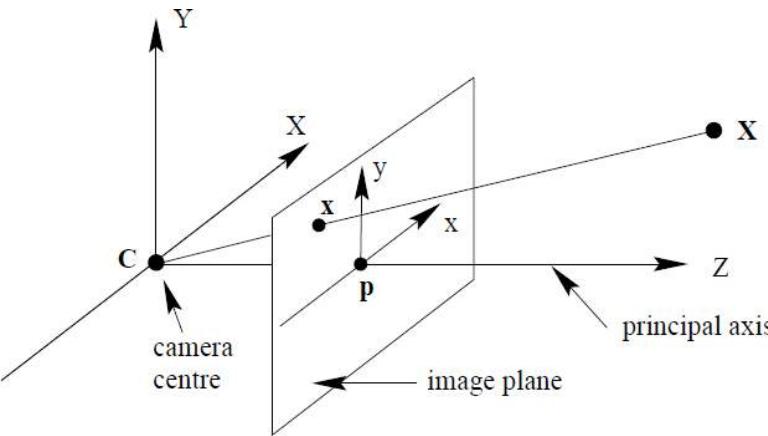
(x, y) ... image coordinates

(X, Y, Z) ... object coordinates

Pinhole camera model

- Intrinsic Parameters

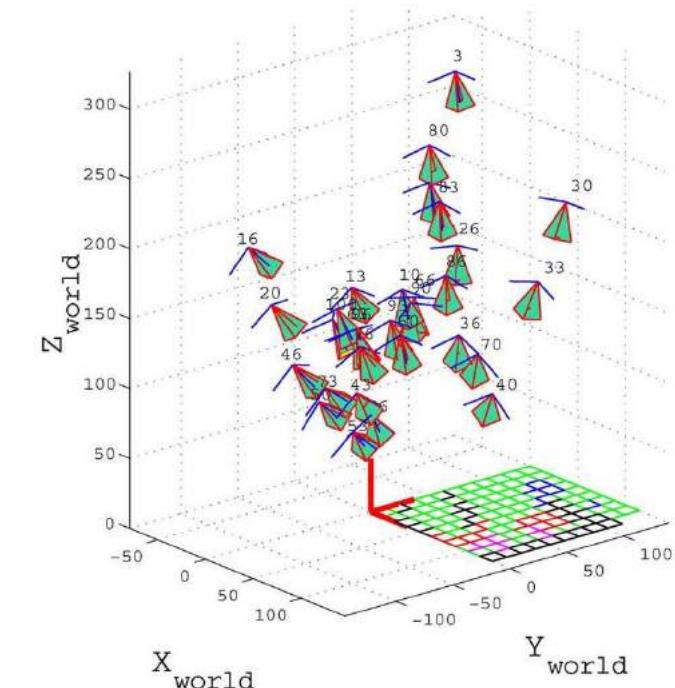
- Focal length (f_x, f_y)
- Principal point (p_x, p_y)
 - Intersection of principal axis with sensor



- Extrinsic Parameters

- Rotation
- Translation (position)

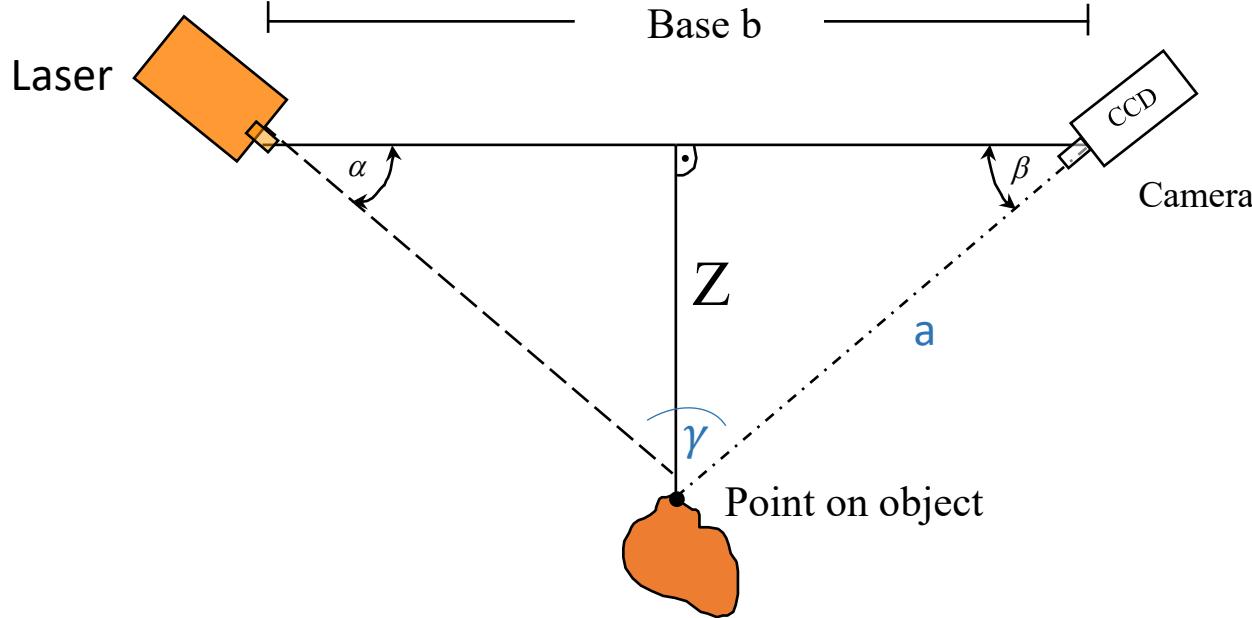
Extrinsic parameters (world-centered)



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Active triangulation - basics



$$\frac{Z}{\sin \beta} = a$$

$$\frac{a}{\sin \alpha} = \frac{b}{\sin \gamma} \Rightarrow a = \frac{b \sin \alpha}{\sin \gamma}$$

$$\frac{Z}{\sin \beta} = \frac{b \sin \alpha}{\sin \lambda} \Rightarrow Z = \frac{b \sin \alpha \sin \beta}{\sin \lambda}$$

$$Z = \frac{b \sin \alpha \sin \beta}{\sin(180 - \alpha - \beta)}$$

- Known Parameters:

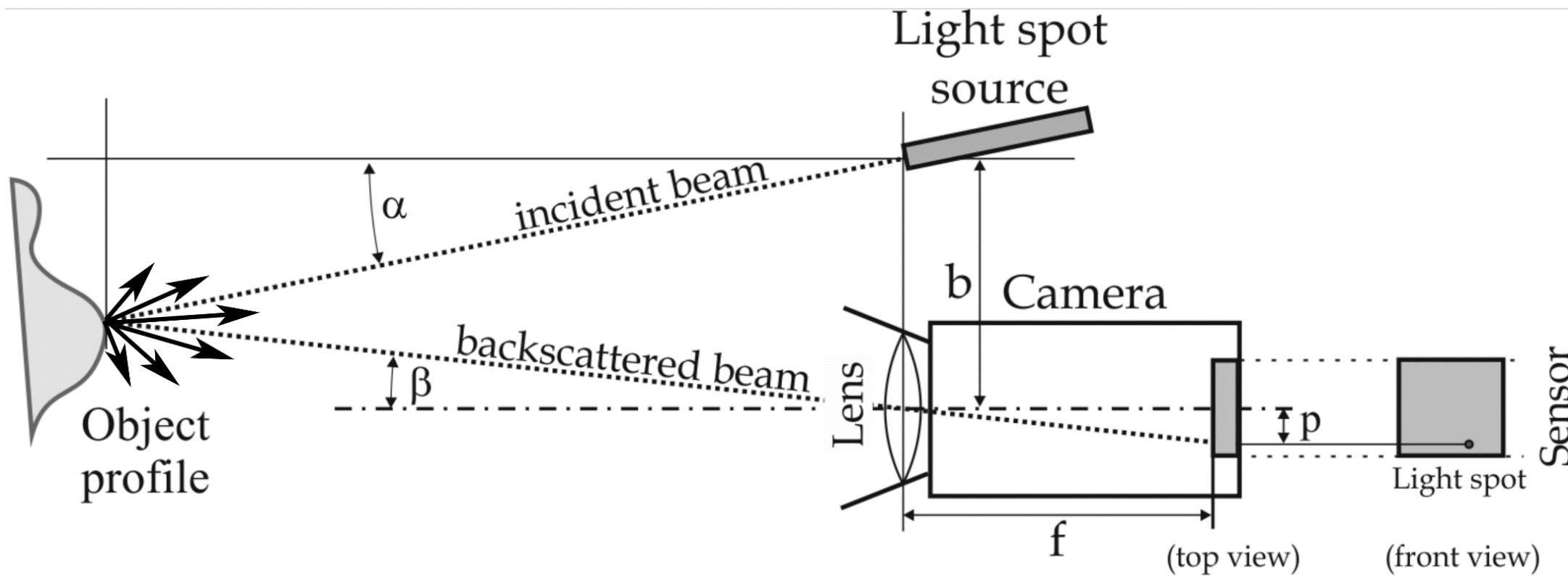
- α : Angle between base and laser beam
- β : Angle between base and light point (seen from camera)
- b : Distance between projector and camera (Base)

- Wanted:

- Z : depth

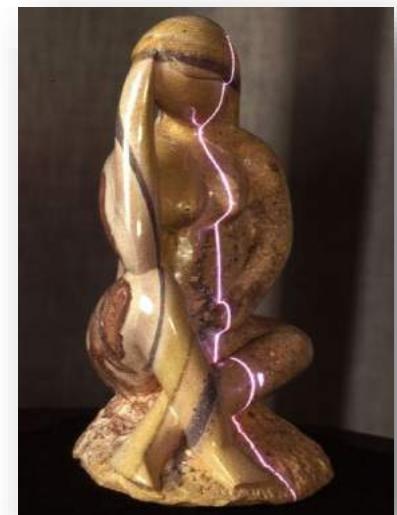
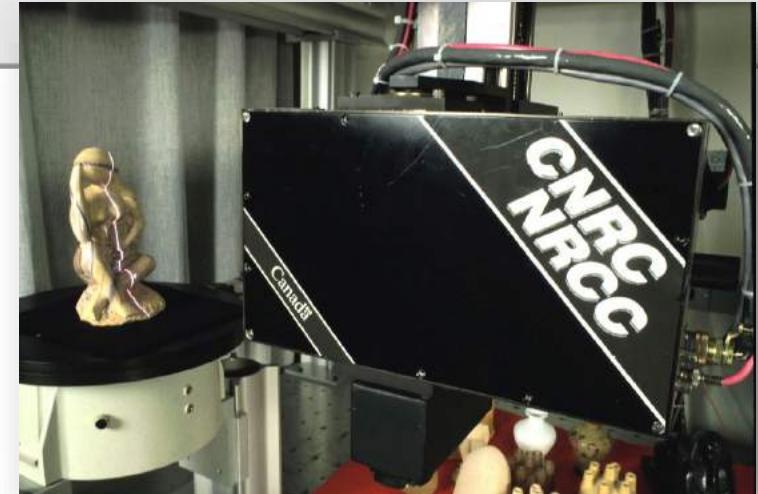
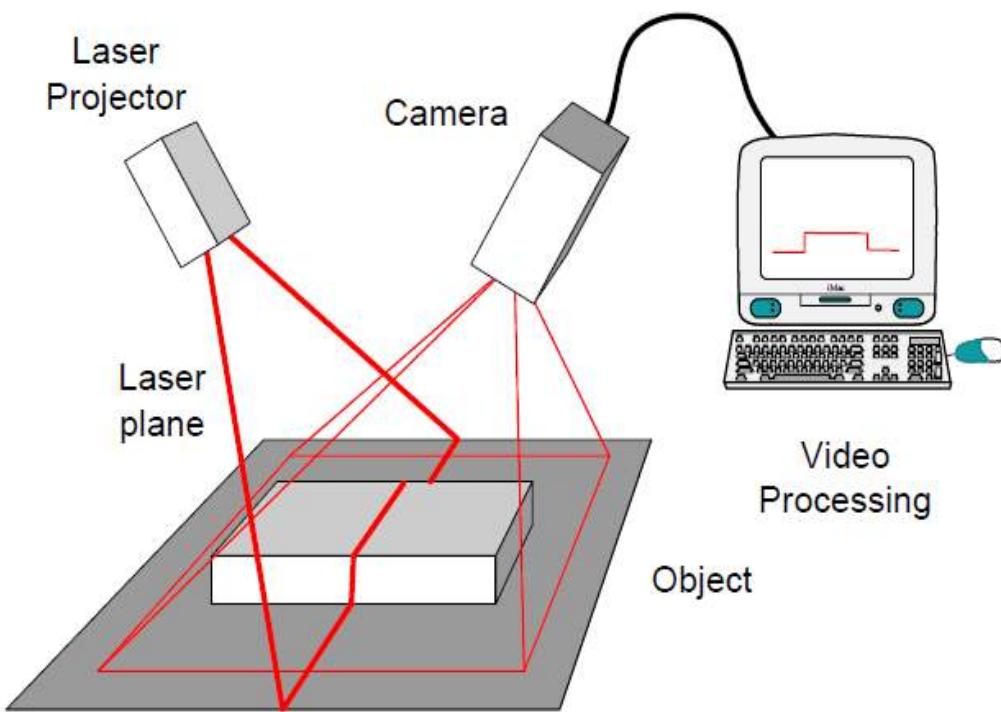
Single Spot

- Laser beam hits the object
- Camera records the position (angle) of the bright spot → single surface point



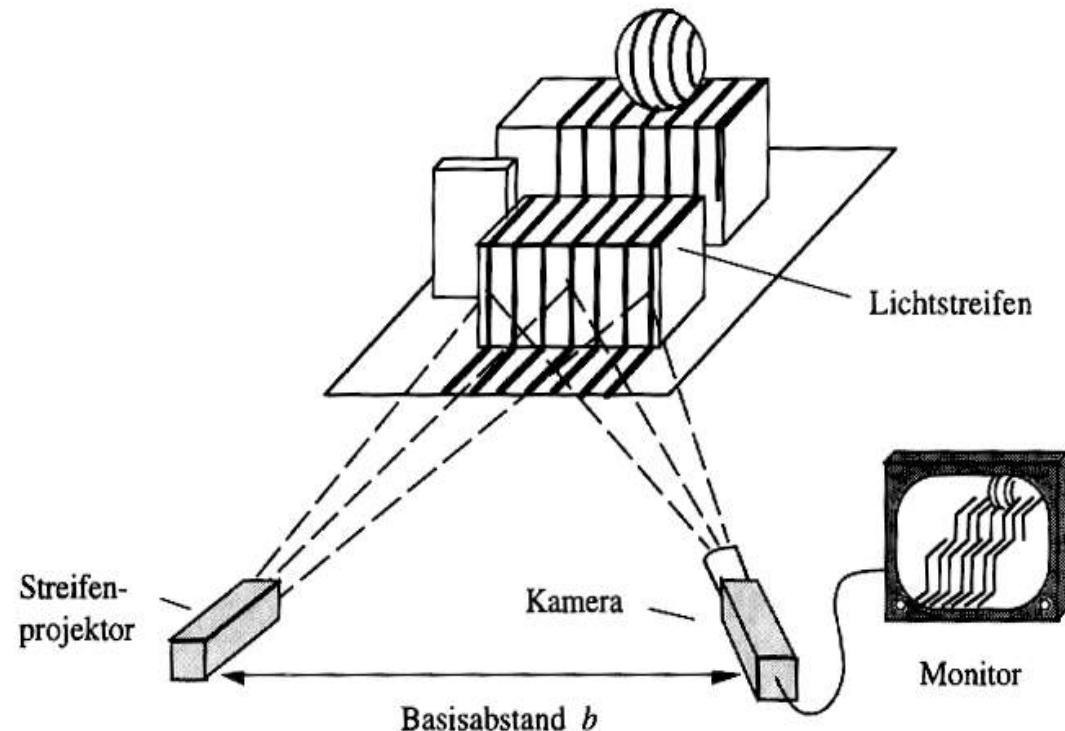
Plane of light

- Laser plane hits the object
- Camera records the bright line → single surface profile



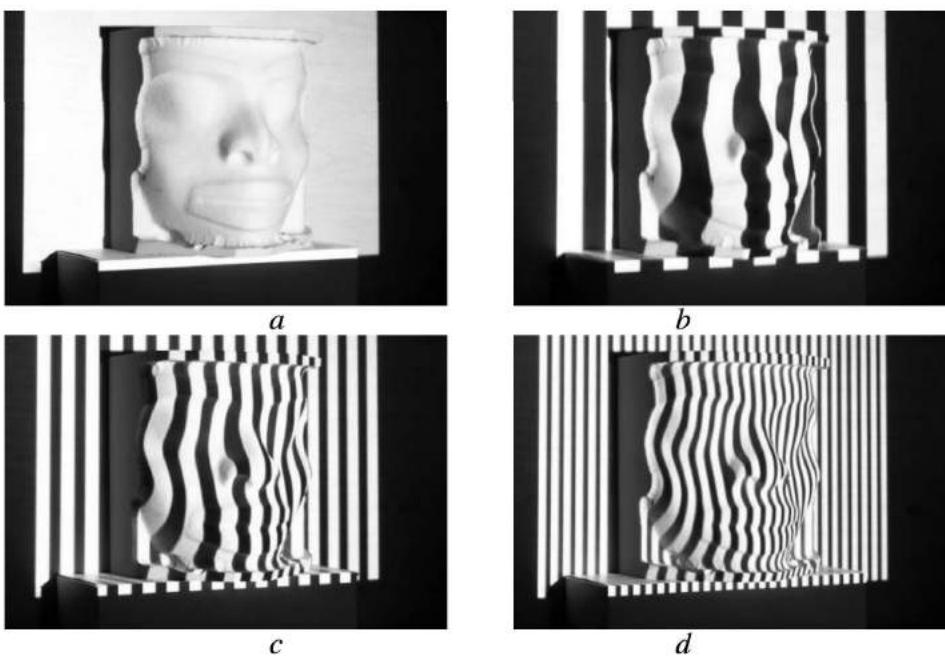
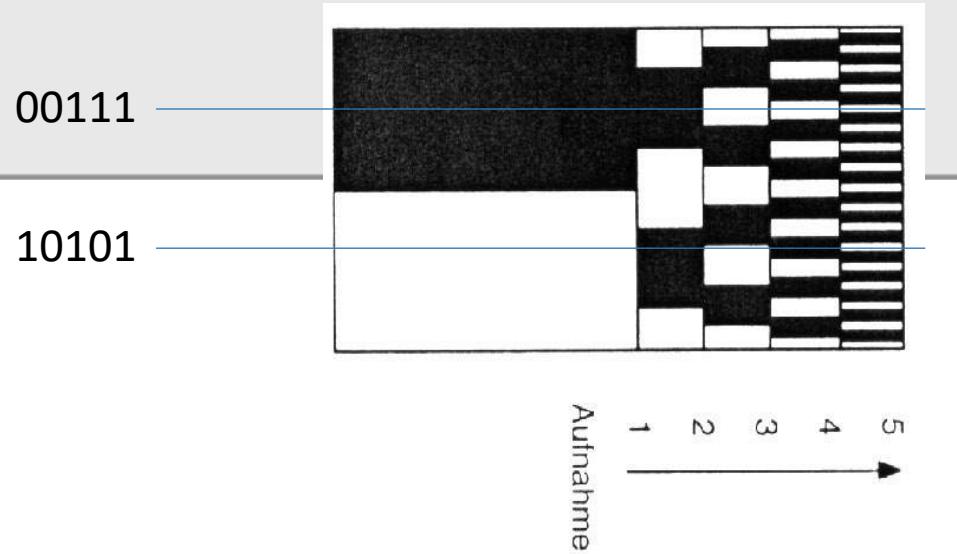
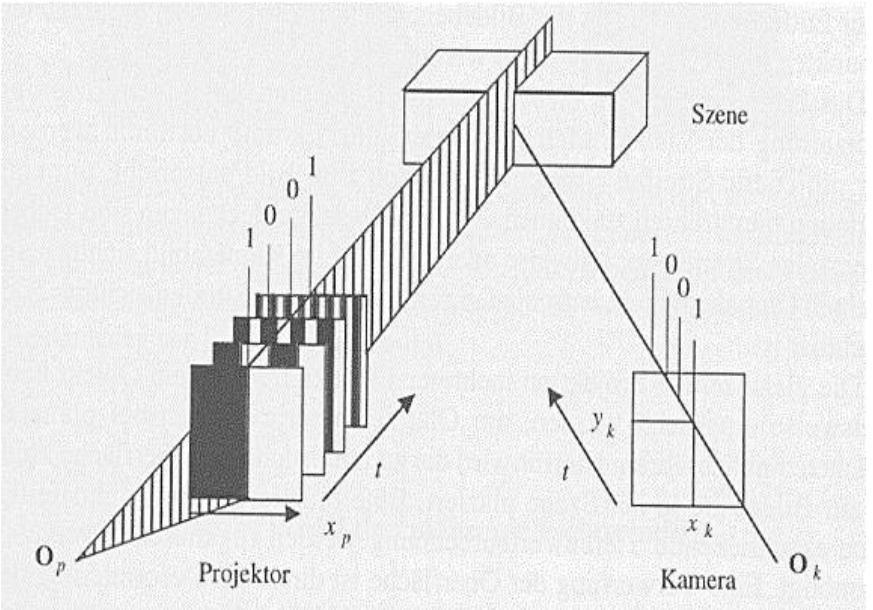
Multiple planes

- Idea: record multiple planes at once, speed up the process
- Problem: parts of strips can be occluded → discontinuities
- no unambiguous identification of light strips possible



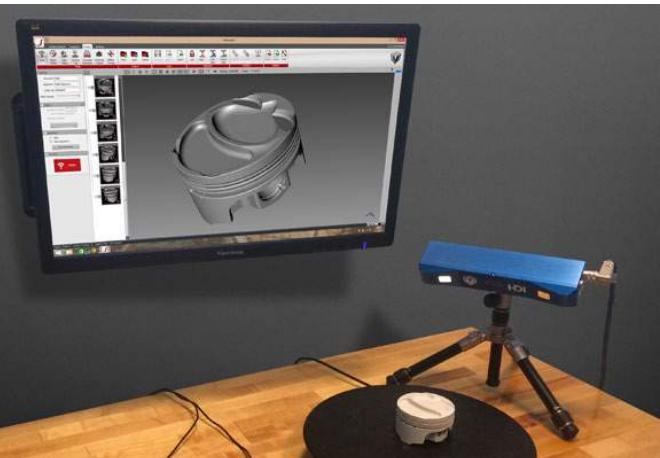
Solution: Gray-code pattern

- Project a sequence of stripes
- Each pixel receives a series of bright/dark intensities → binary code
- Unique localization in the pattern possible

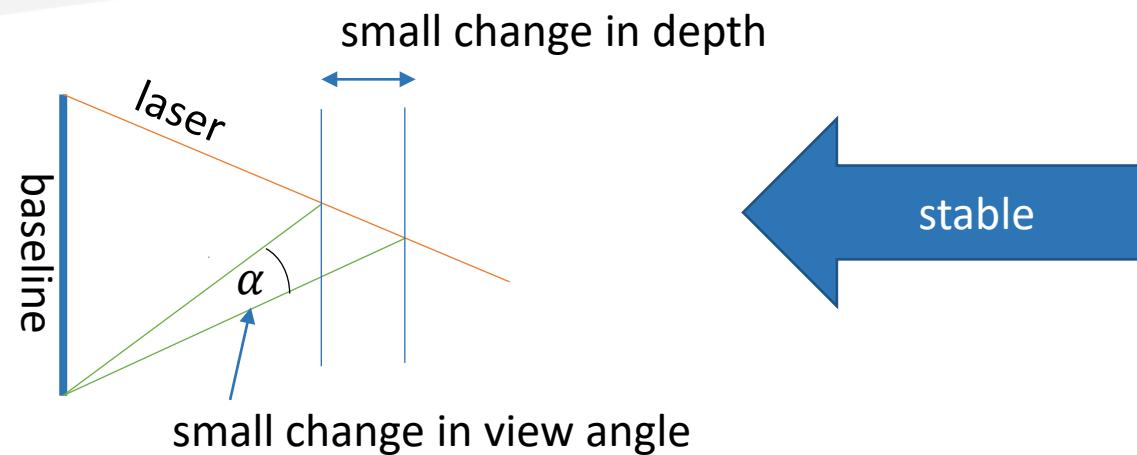


Active Triangulation – applications

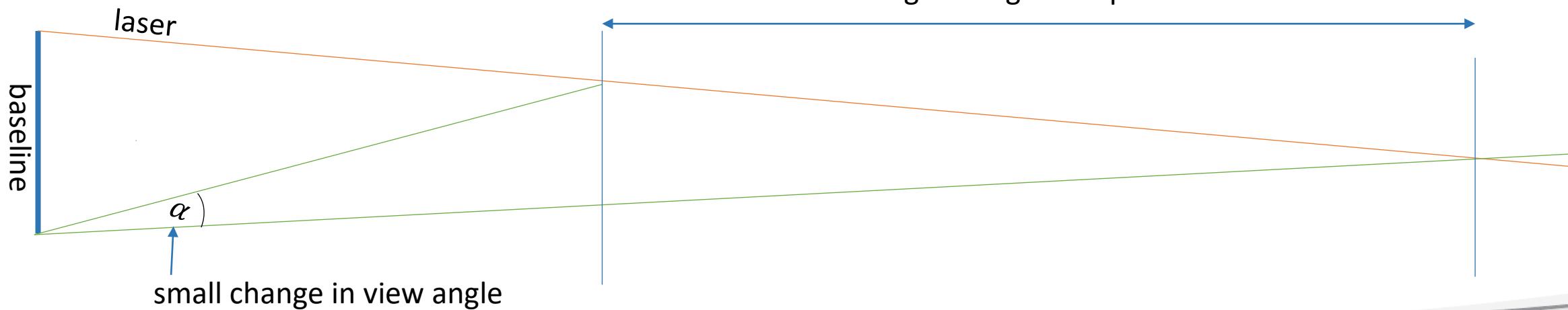
- Rather for close-range applications
- Archaeological objects, industrial applications
- High accuracy (micrometers)



Why are long ranges problematic?



Larger ranges require larger baselines

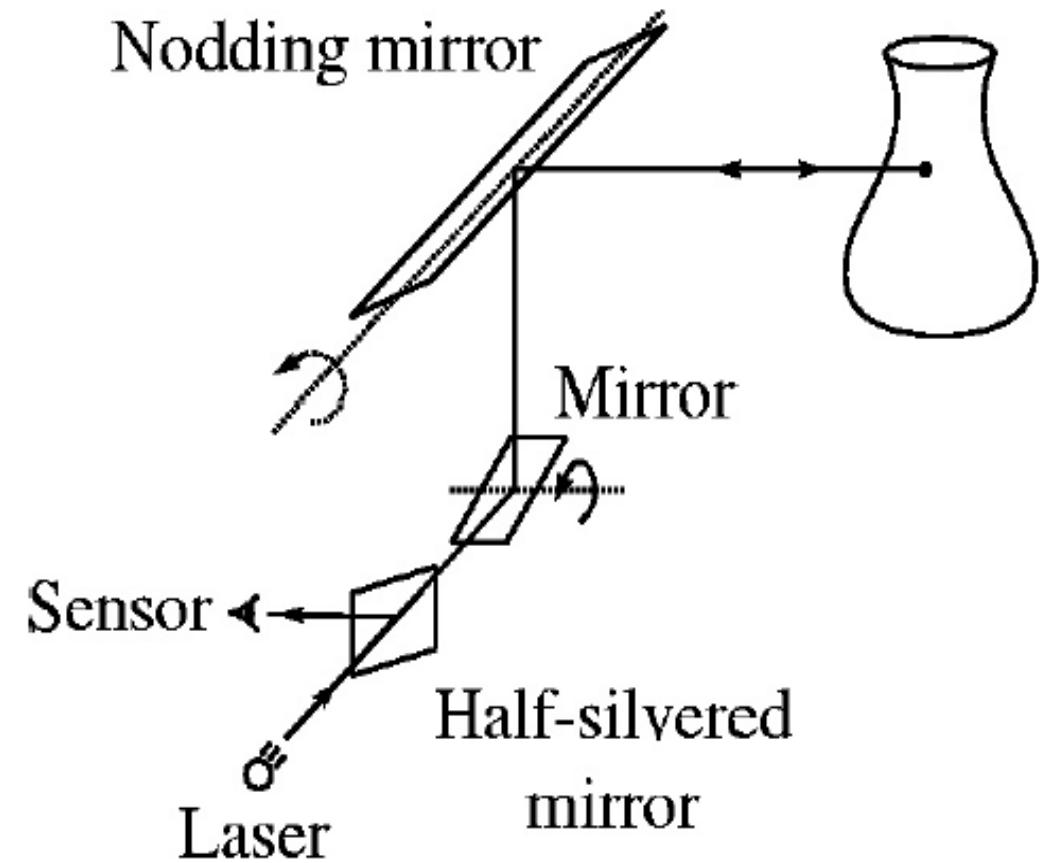


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Range scanners – Time of Flight

- Shoot a light pulse at the object and measure the time until its reflection is measured
- “LIDAR” (Light Radar, Light Detection and Ranging)
- $d = \frac{c * \Delta t}{2}$
- c... speed of light
- Accuracy of time measurement is limiting factor

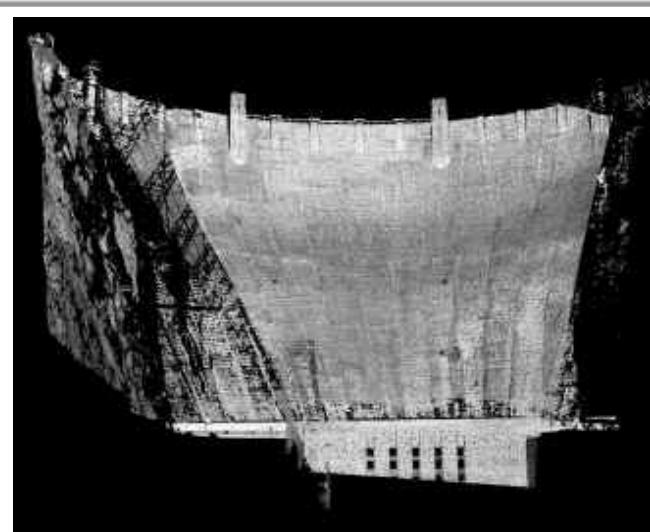


Range scanners – Time of Flight

- For long ranges
- Accuracy in mm-cm area
- Also airborne applications



cyrax

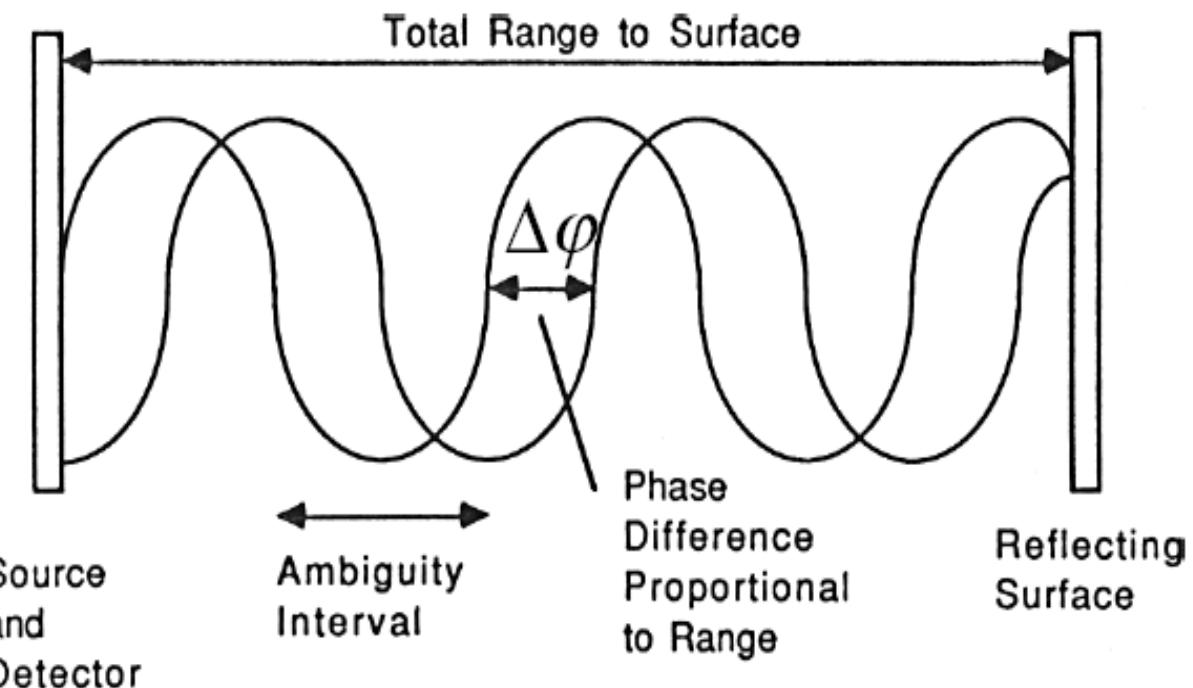
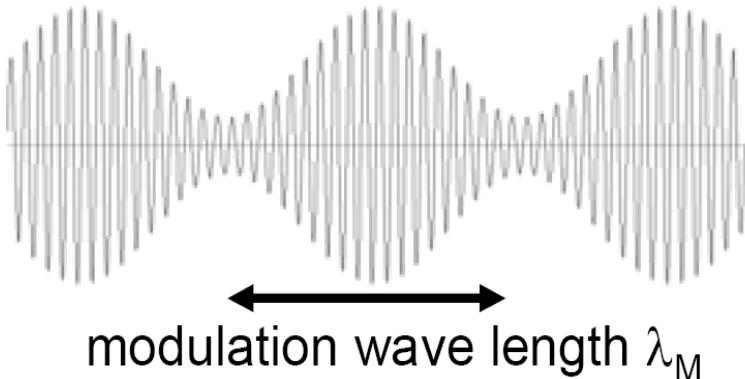


Mensi GS100



Range scanners – phase difference

- AMCW: Amplitude-Modulated Continuous Wave
- Measure the phase difference between emitted and measured wave
- Ambiguity if distance is longer than modulation wavelength



Range scanners – phase difference

- Medium distances → ambiguity interval
- Accuracy in mm area



Zoller Fröhlich IMAGER 5300



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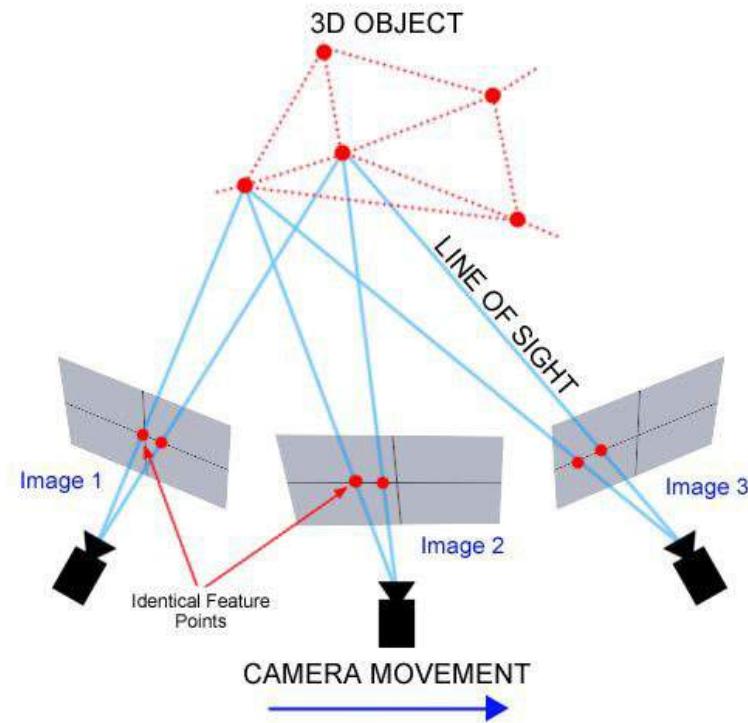
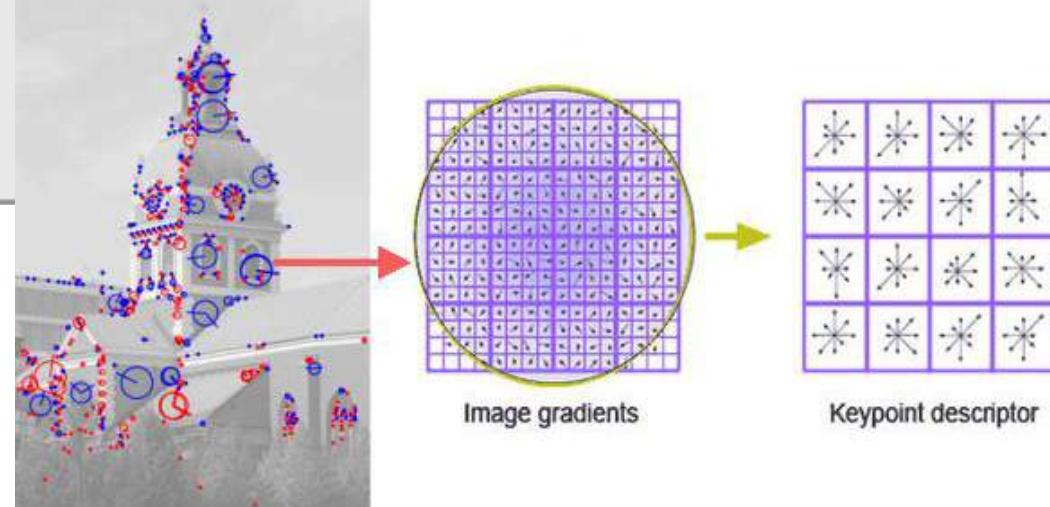
Photogrammetry

- Reconstruct the shape from a set of images, taken from different positions
- Passive method - no additional light / radiation is introduced
- Depth estimation via triangulation
- **Relies on finding corresponding points in different images**



Photogrammetry – Basic algorithm

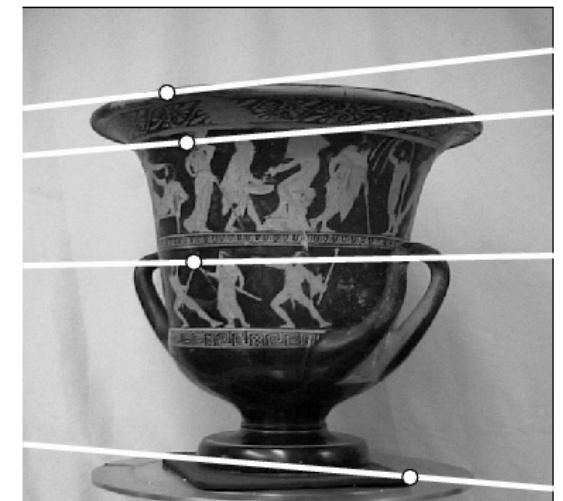
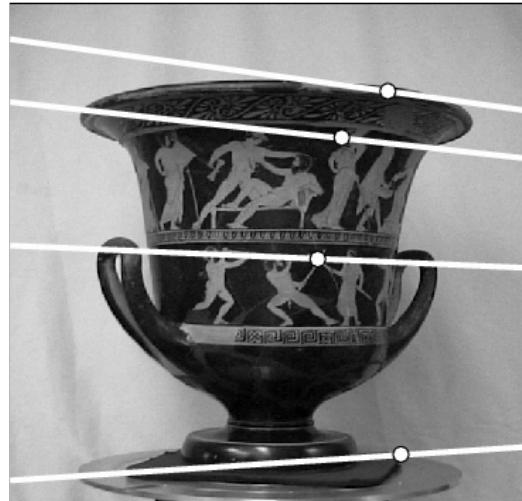
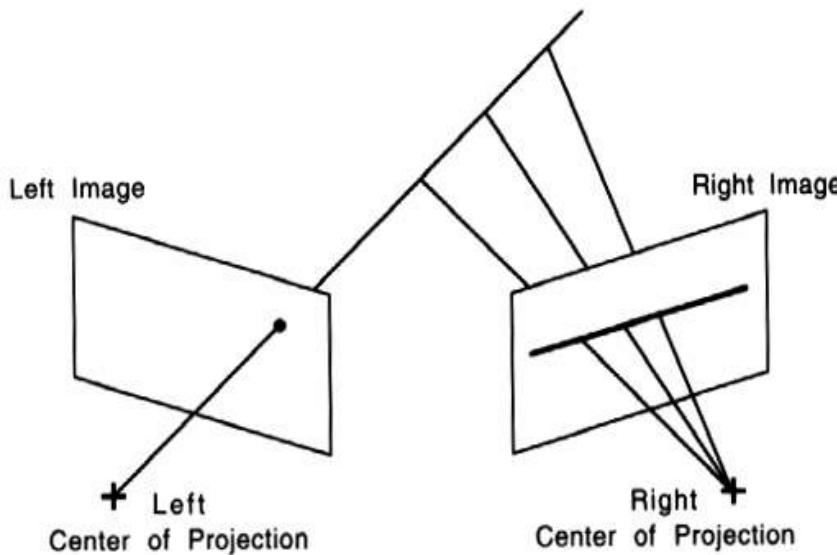
1. Find **matching points** between images
 - a) Detect distinctive points in each image
 - b) Compute descriptors for each point
 - c) Find best matching points between images
2. Estimate camera position & orientation for each photo



Photogrammetry – Basic algorithm

3. Dense reconstruction

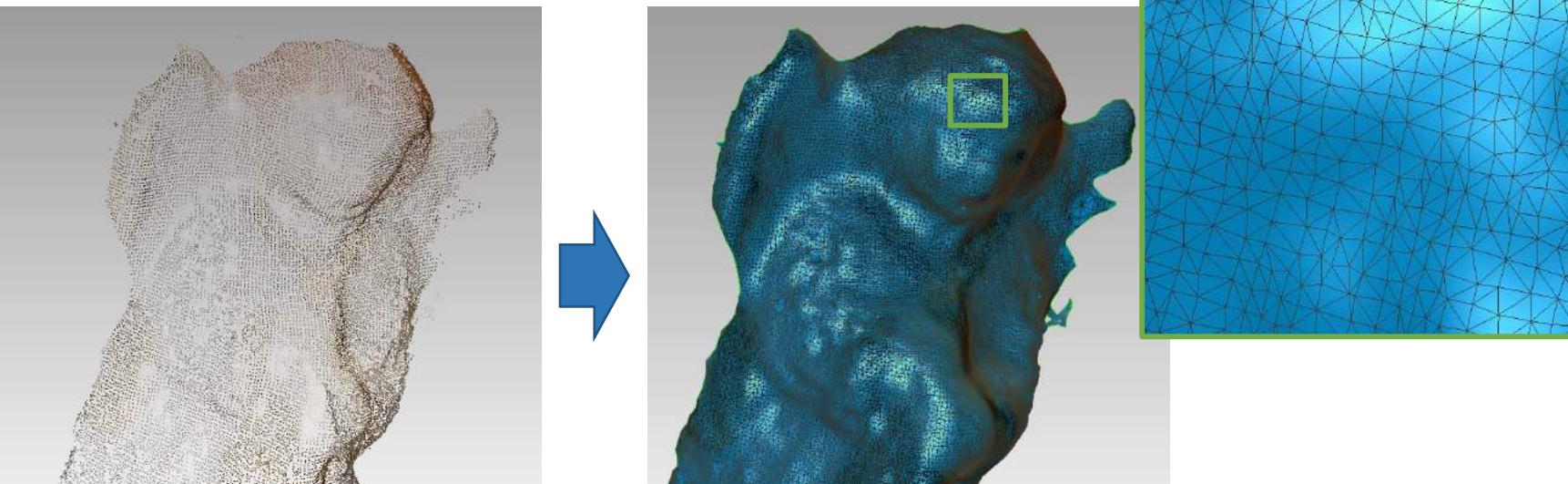
- a) Knowledge of camera poses simplifies the point matching problem
- b) **Epipolar geometry:** a point in one image corresponds to a line in the other image
- c) Search for matching points only along epipolar lines
- d) Triangulate point positions



Photogrammetry – Basic algorithm

4. Surface reconstruction:

Unordered 3D Points → Surface Mesh



How to Photogrammetry

1. Check if the method is applicable for your object
2. Take **good** photos (most difficult and important)
3. Process them with a Photogrammetry Software, e.g.:
 - Agisoft Metashape (commercial)
 - Meshroom (open source)
4. (optional: editing)
5. Marvel at your results!

1. Applicability

Don't:



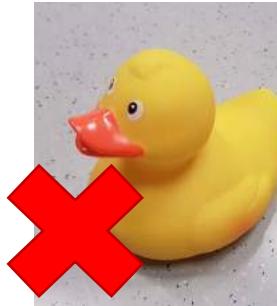
Shiny



Transparent/translucent

Here the surface color depends
on the angle of view!

No unique point
matches possible!



Smooth, uniform surfaces



Deformable

Shape might change during
acquisition!

Do:

- "Natural" materials
 - Wood
 - Stone
 - Clay
 - ...
- Corroded / worn materials
- Ragged, irregular surfaces



2. Take good pictures

- If you want nice results, invest some time & effort here!
- Different acquisition strategies for different applications

Fixed camera, rotating object



Moving camera, fixed object

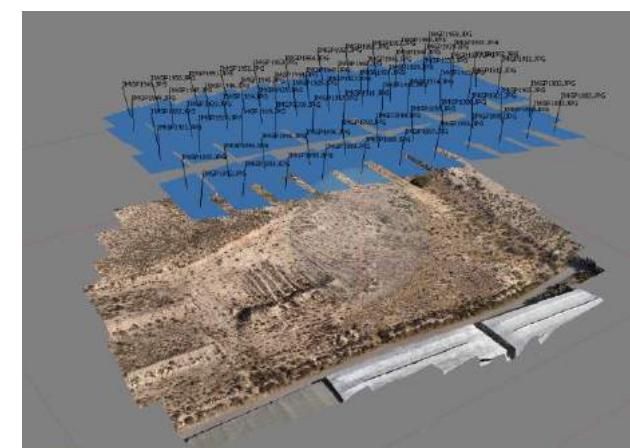


Multiple synchronized cameras – nothing moves



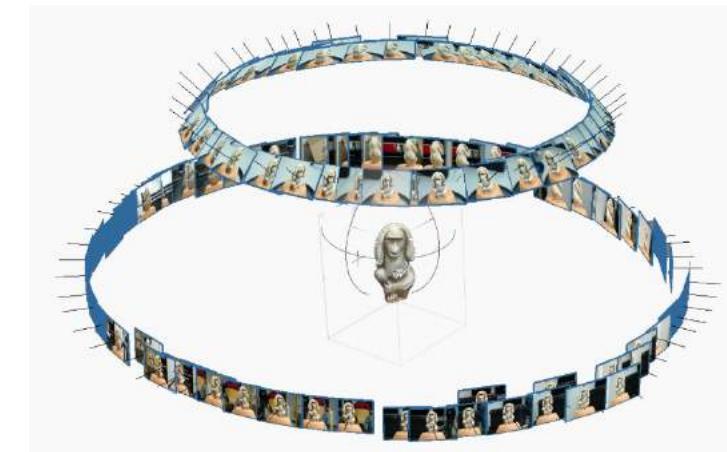
Recommended for beginners: object fixed, camera moving

- Minimal setup efforts, very versatile
- Applicable for a wide range of objects
 - Small artifacts, buildings, excavation sites, cities...
- Applicable in a wide range of environments
 - Indoors, outdoors, airborne (e.g. with drones)...



For smaller objects

- Put your object somewhere accessible (stand, stool, etc.)
- Walk around the object in $\sim 10^\circ$ steps \rightarrow 1 full round = ~ 36 pictures (approximately – no need to measure that)
- Do this from 2-3 elevation angles
- NEVER MOVE THE OBJECT during acquisition
 - relation between object and background must not change
 - Different position \rightarrow different shadows \rightarrow different surface color
- Try to keep approx. the same distance
- If possible/necessary: Turn the object upside down and repeat (to capture the bottom side) - this will result in a separate model!



For larger objects (buildings, etc.)

- Walk parallel to the wall/object surface
- Consecutive images should overlap by min. 80%
(remember: to reconstruct a point, it must be visible in min. 2 images!)
- Good idea: find out how many steps you should take between two shots
- Sometimes turn left and right to
 - increase overlap areas
 - Create larger baselines
 - Reach blind spots

$$\frac{\text{sensor size}}{\text{coverage}} = \frac{\text{focal length}}{\text{object distance}}$$

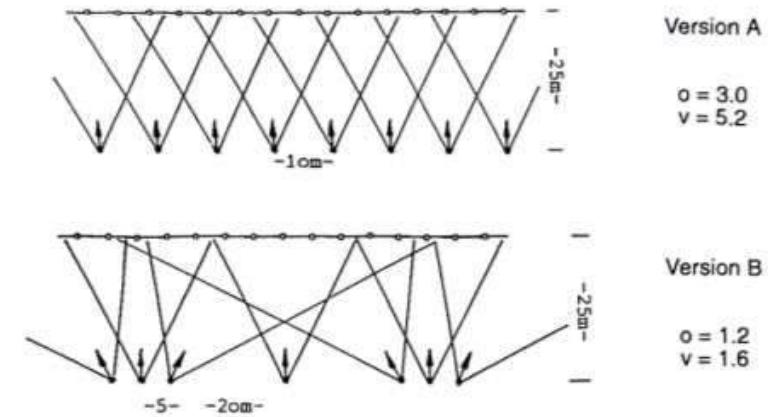


Figure 4.5-3: Camera dispositions for the LONG WALL

Taking photos – general advice

- Use a "real" camera
 - DSLR, mirrorless,...
- Shoot in manual mode, keep camera parameters constant
- Don't change the focal length (zoom)
- Care about illumination
 - Enough light!
 - Smooth, uniform
 - **Life-hack: shoot outdoors on a cloudy day!**



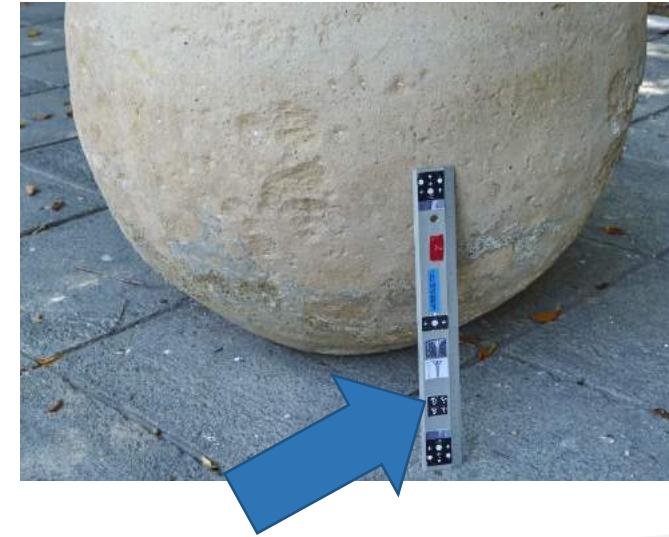
Use a small aperture

- Most of the object should be in focus
- Small aperture (=high f-number) → large depth of field
- This can lead to longer exposure times → Use a tripod!



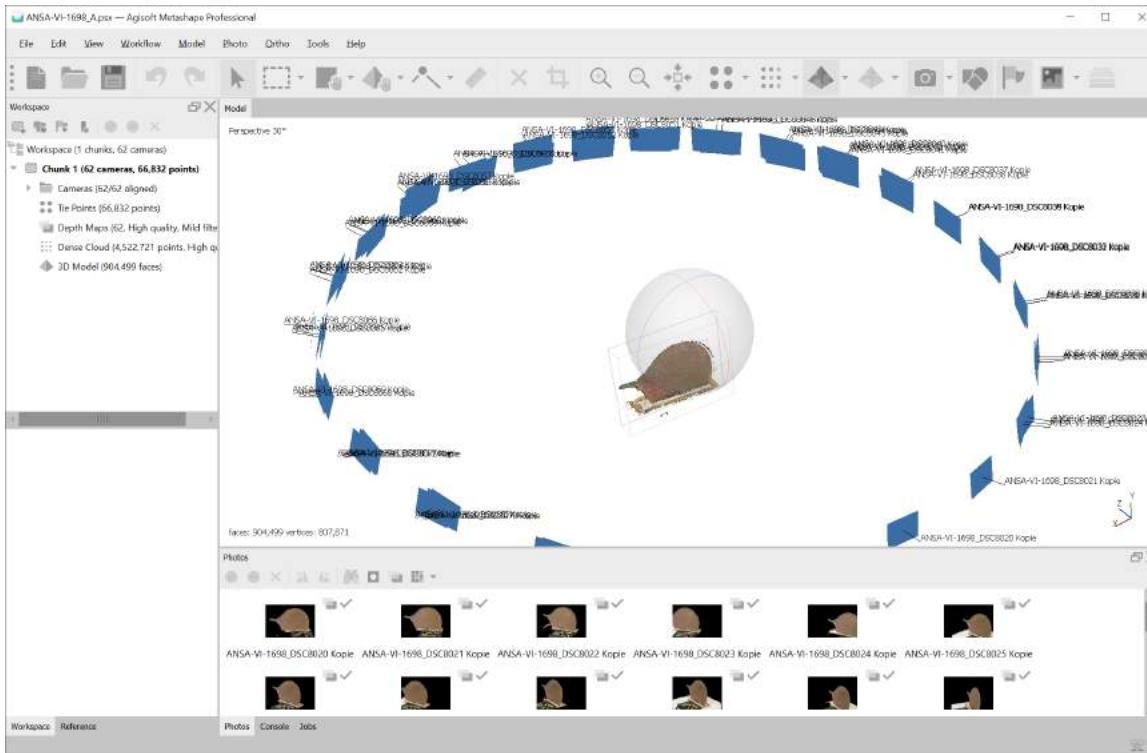
Put a reference object in the scene

- Necessary to correctly scale your model
 - Grid
 - Ruler

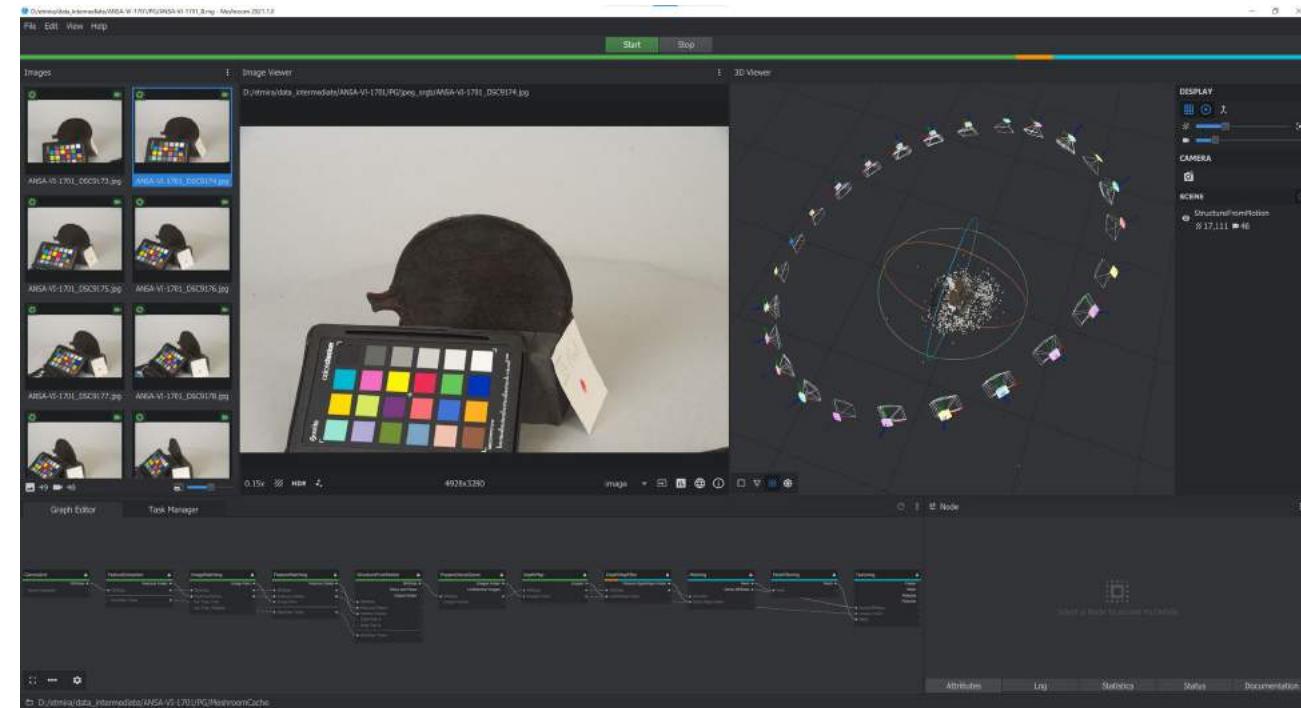


3. 3D Reconstruction

- Just use an existing software tool and follow the manual...
 - My favourites:



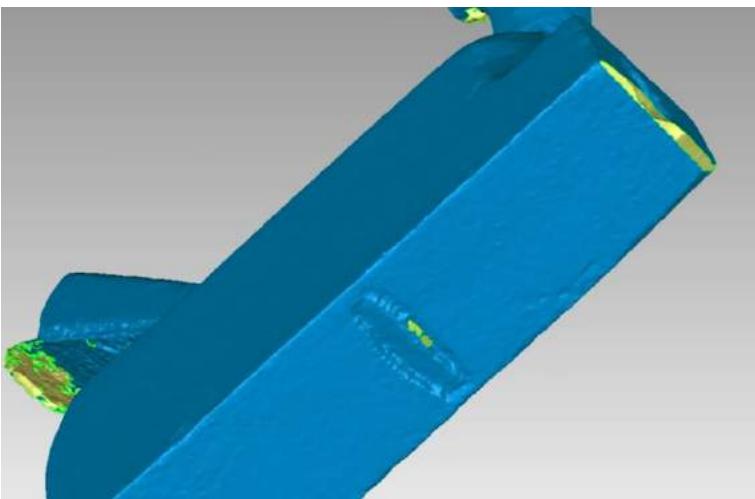
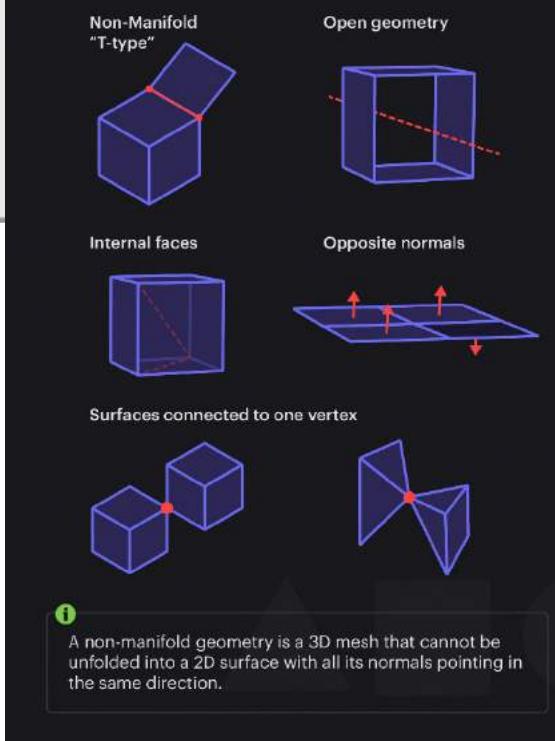
Agisoft Metashape Professional (30 days free trial available)



Meshroom (open source!)

4. Editing

- Close holes
- Remove unnecessary parts
- Repair broken geometry
 - Broken normal vectors
 - Non-manifolds
 - Overlaps/intersections
- Professional software: *Geomagic Wrap*
- Free options:
 - *Autodesk Meshmixer*: very user friendly, a bit limited
 - *Blender*: 3D modelling software – very powerful, steep learning curve
 - *Meshlab*: many features, a bit overwhelming for the non-scientific user



5. Marvel at your results

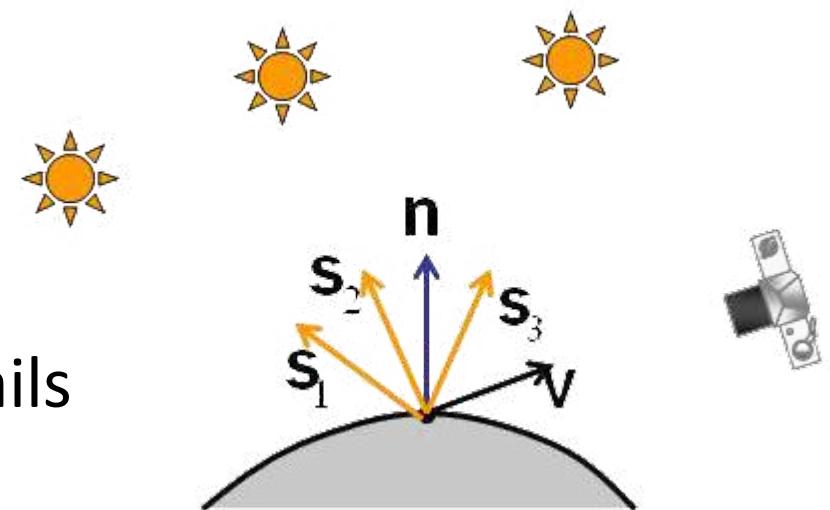


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Photometric Stereo

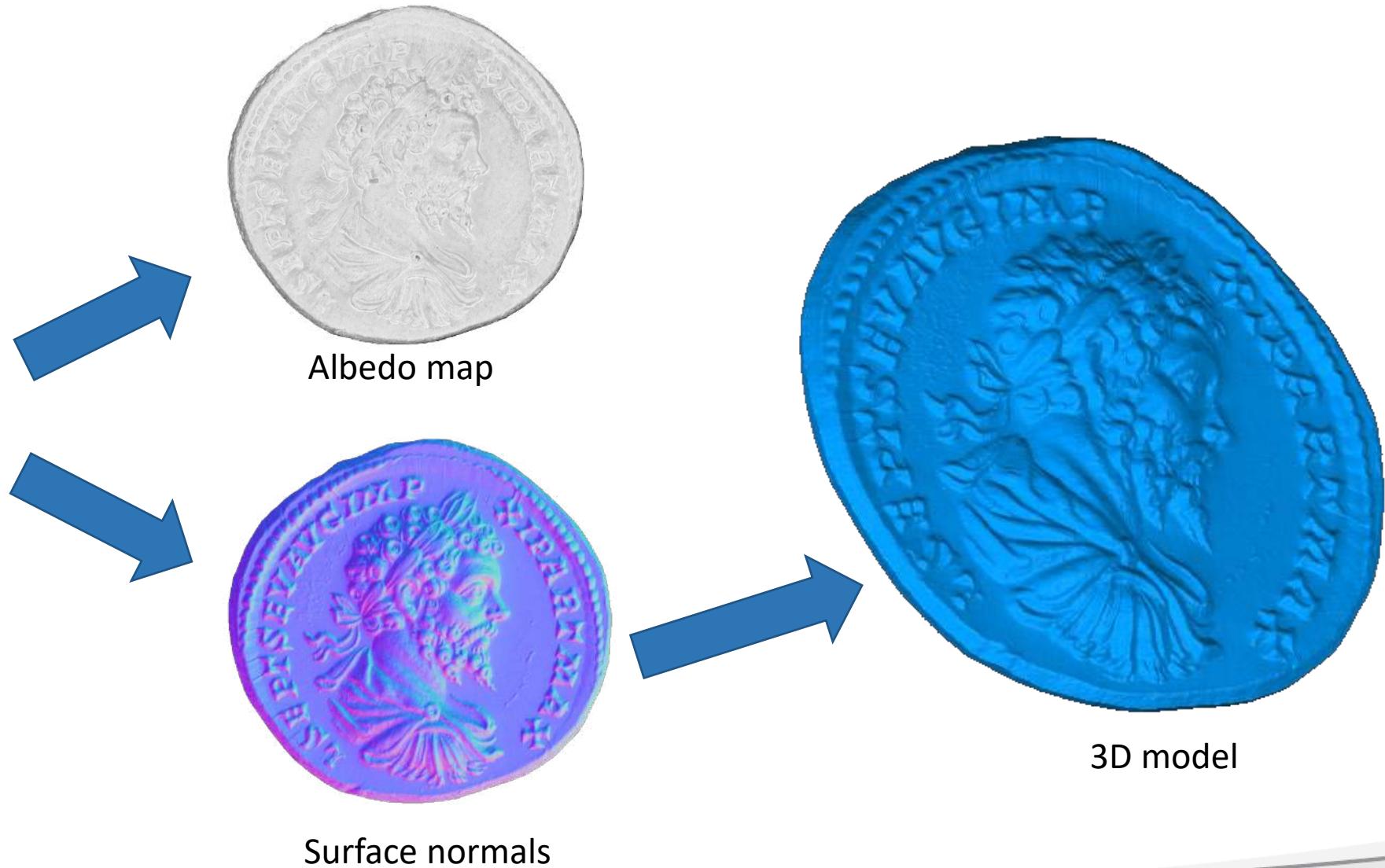
- Reconstruct 3D surface from multiple raking light images
- Advantages (over other 3D reconstruction techniques):
 - Relatively cheap and simple acquisition
 - Spatial resolution only limited by resolution of input images
- Disadvantages
 - Susceptible to low-frequency-noise
→ distorted global shape
 - Ambiguities
- → good option for quasi-flat objects with fine details
 - Such as manuscripts...



Example



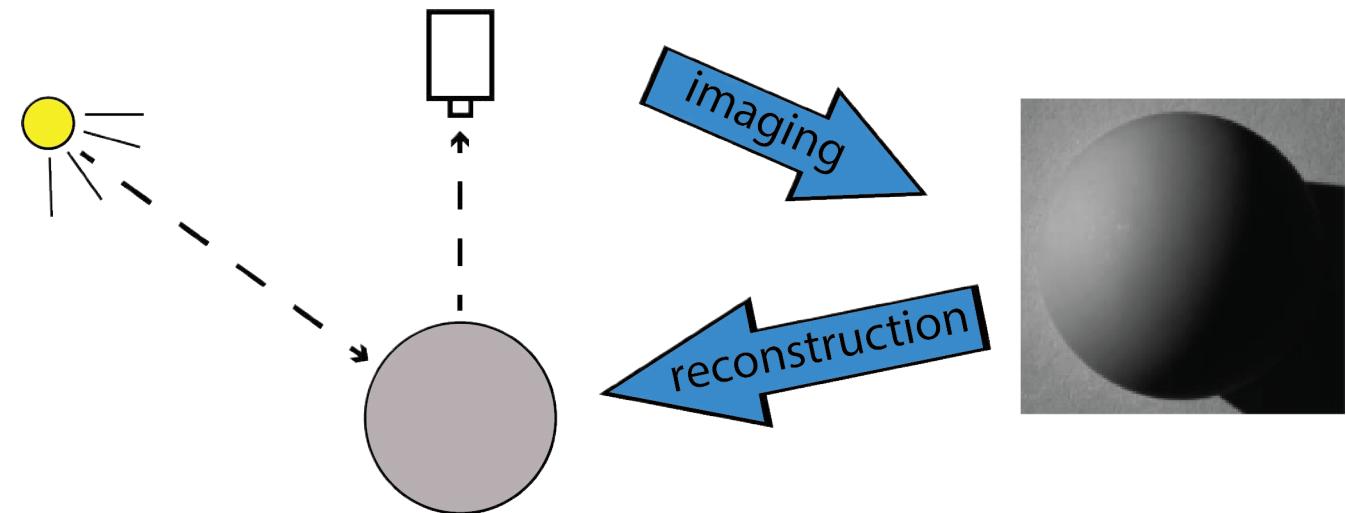
Input images



Shape from Shading vs. Photometric Stereo

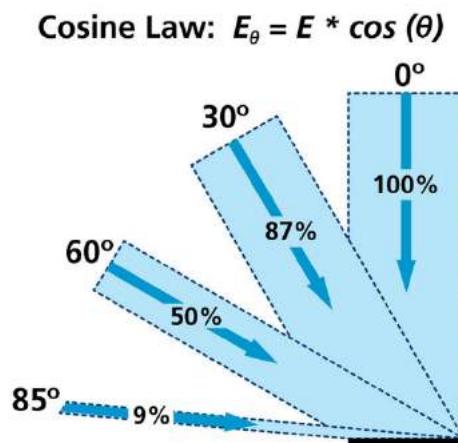
- Single input image: „Shape from Shading“

- Estimate surface inclination from brightness values
 - Reverse imaging process
 - ill-posed problem, highly ambiguous



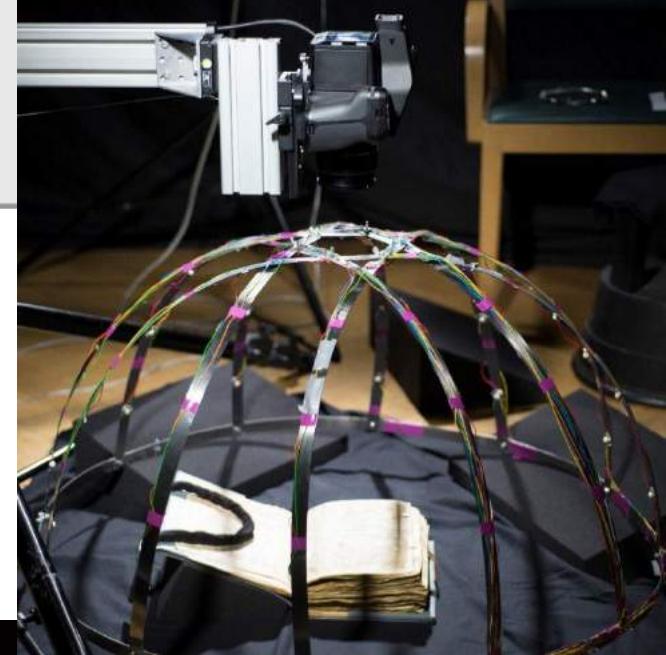
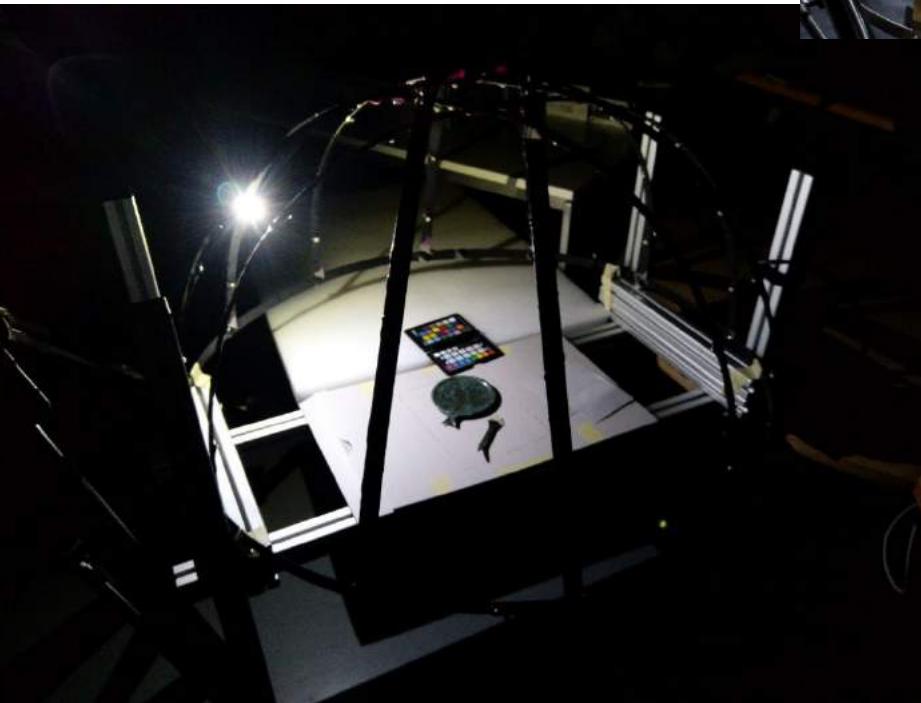
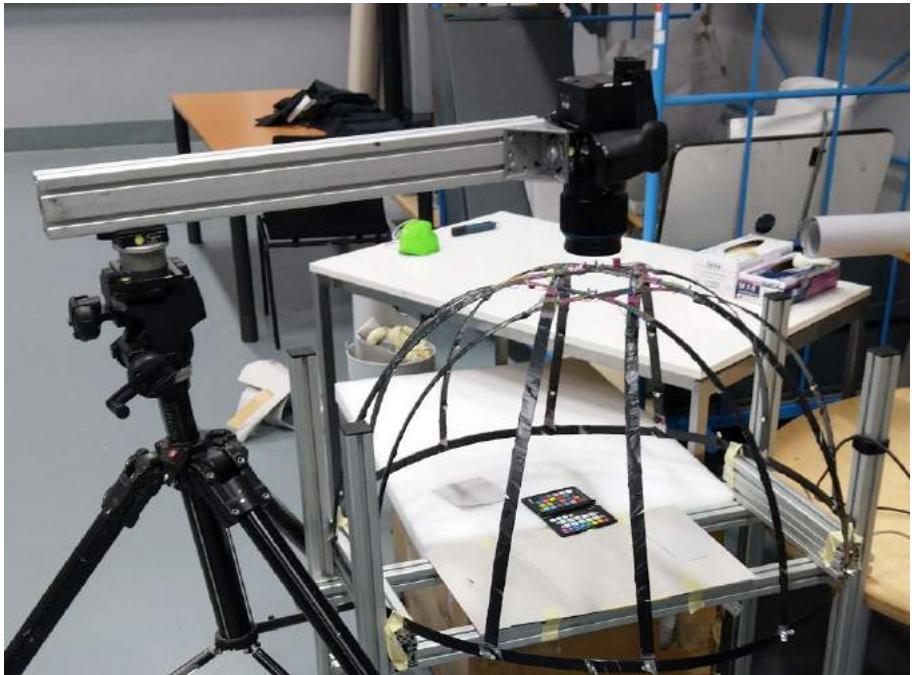
- Multiple input images: „Photometric stereo“

- lit from different directions
 - Unique solution possible

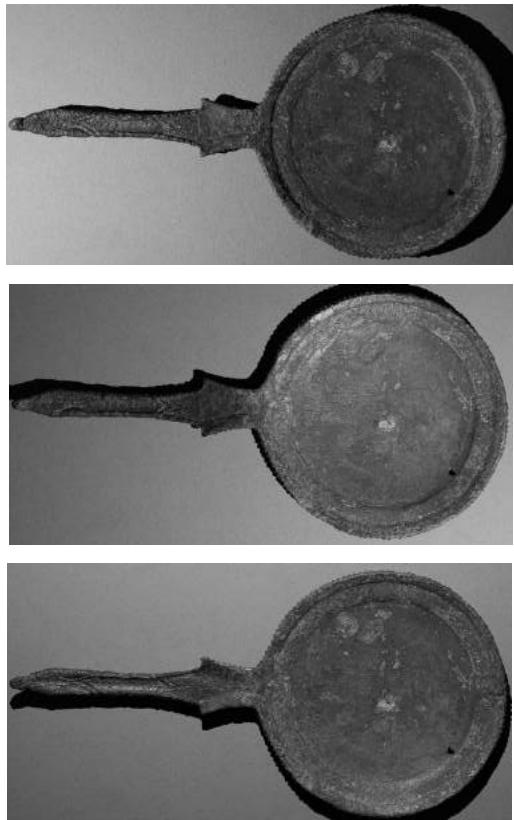


Example setup: light dome

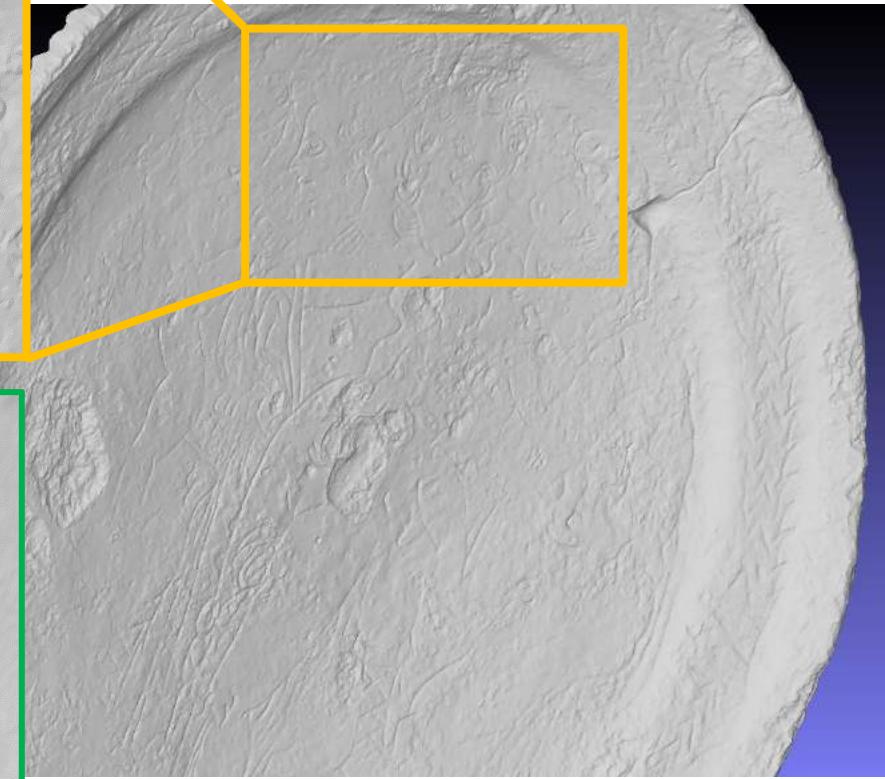
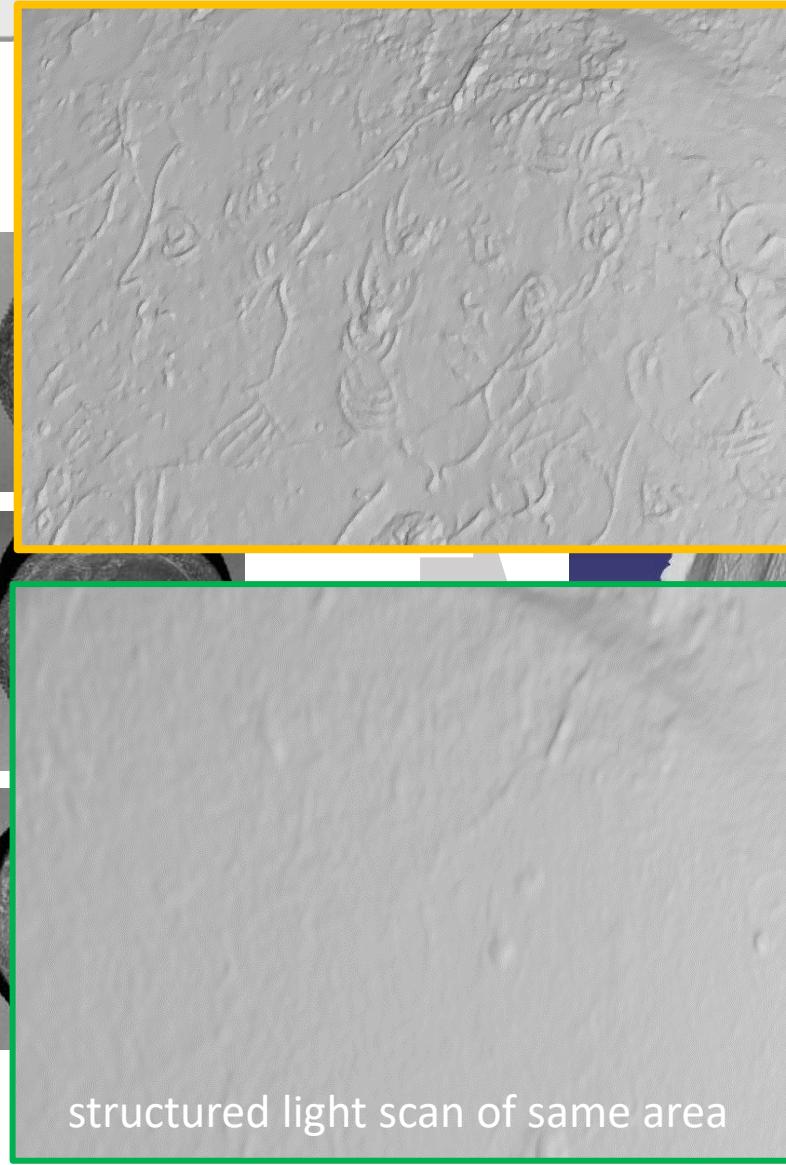
- 54 high-power LEDs in a dome structure
- Open design for easy object handling



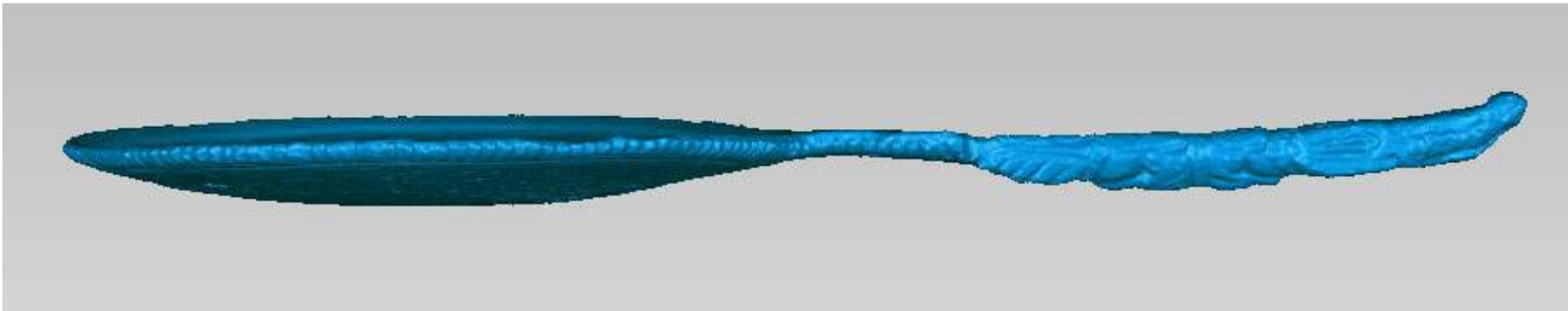
Photometric Stereo vs. Structured Light – Surface details



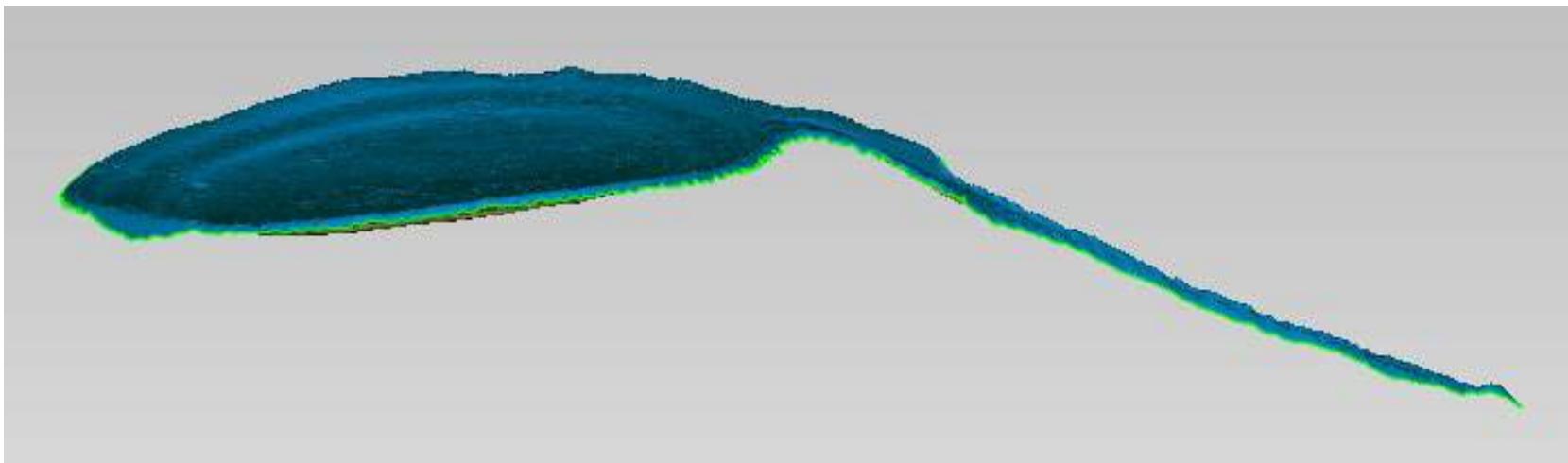
...



Photometric Stereo vs. Structured Light – Global shape



Structured Light

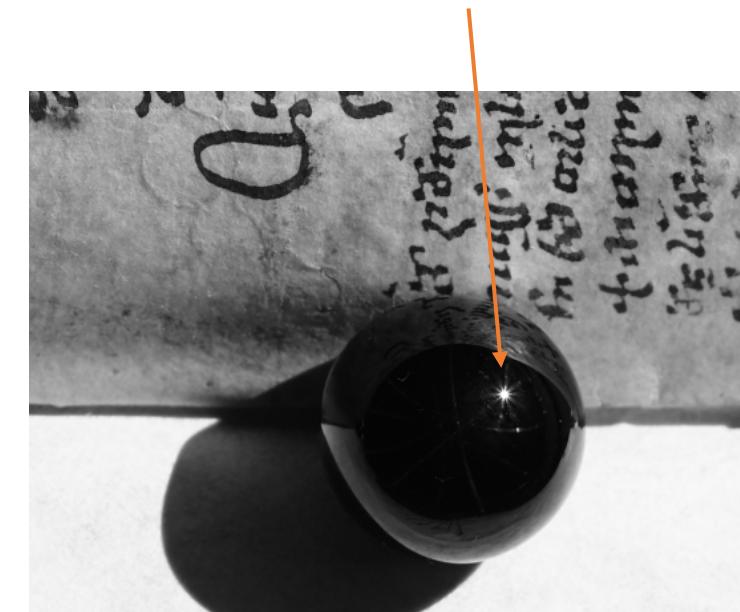


Photometric Stereo

Related: Reflectance Transformation Imaging (RTI)

- Same kind of input images as photometric stereo
- Result: reflectance model
 - Interactive re-lighting
 - Enhancement of details
 - **No real 3D information**
- Free tools available:
 - RTI Builder (creating the model from input images)
 - https://culturalheritageimaging.org/What_We_Offer/Downloads/Process/index.html
 - Needs **reflective balls** in the input images!
 - RTI Viewer (viewing the model)
 - https://culturalheritageimaging.org/What_We_Offer/Downloads/View/index.html

Highlights indicate light directions

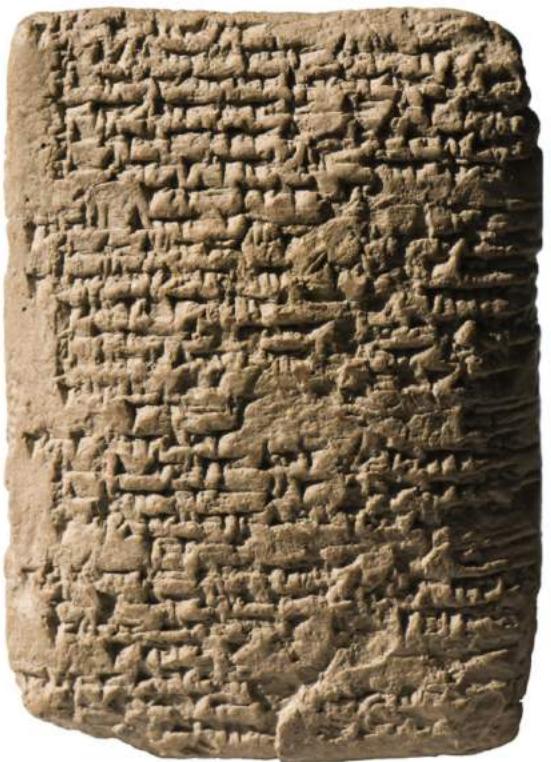




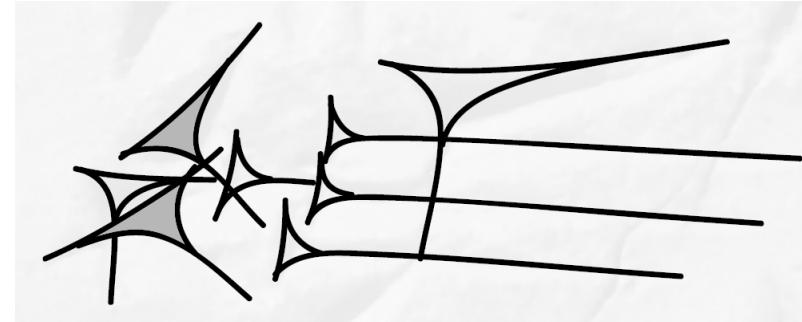
Lecture Outline

- Introduction
 - Why 3D reconstruction?
 - Basic concepts
- Reconstruction Approaches
 - Active triangulation
 - Range scanners
 - Photogrammetry (with how-to)
 - Photometric Stereo
- Application to written heritage
 - Examples from research

Cuneiform recognition



vectorization



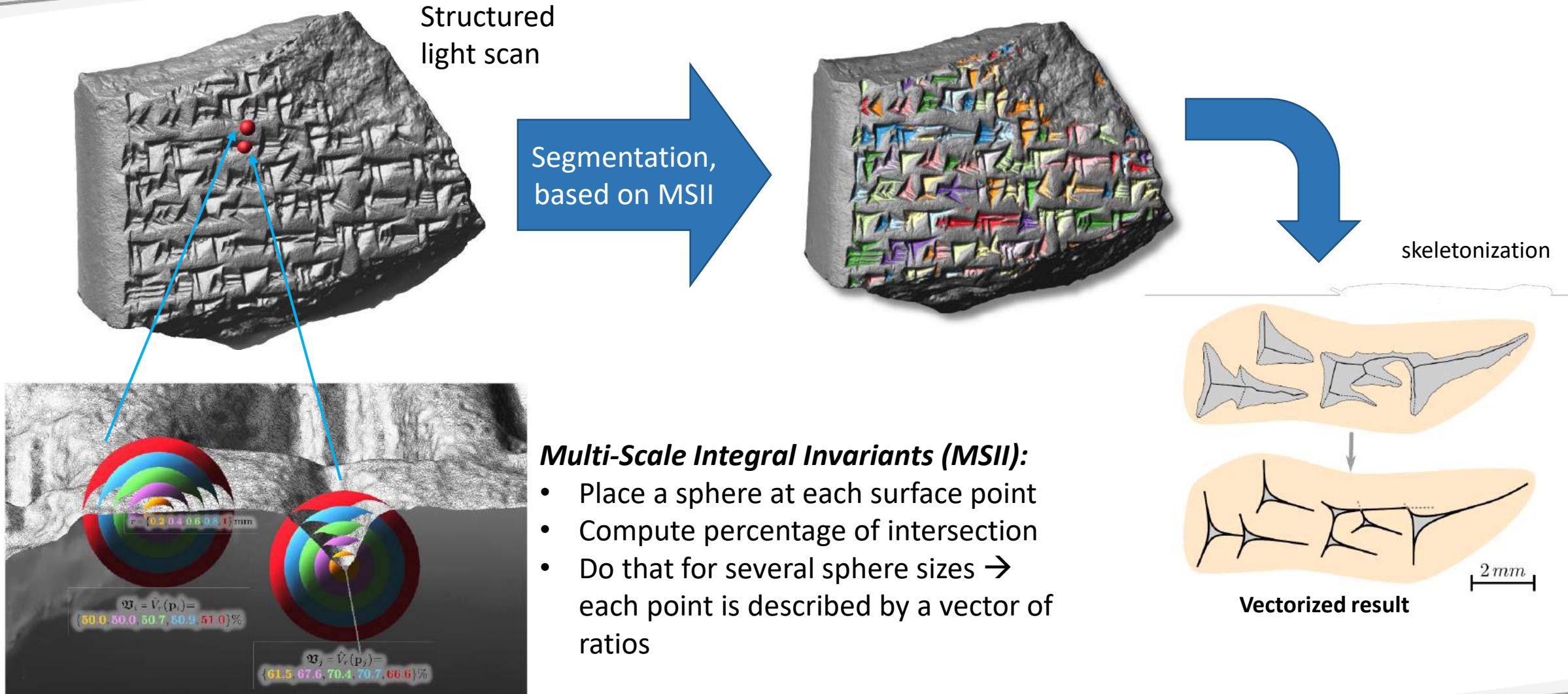
recognition

„ka“

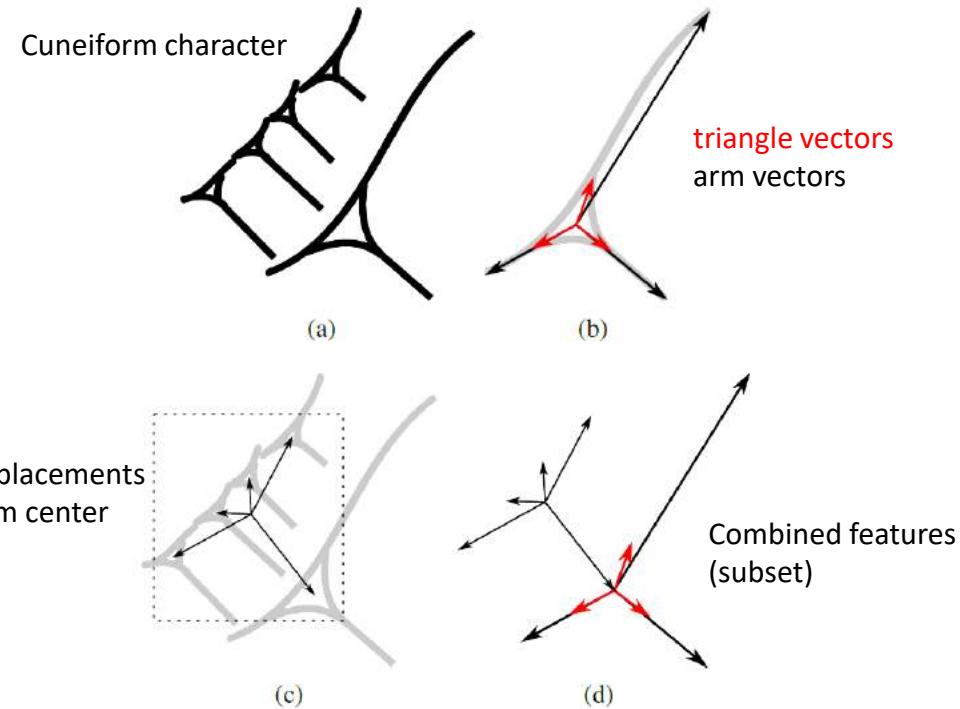
H. Mara and S. Kromker, "Vectorization of 3D-Characters by Integral Invariant Filtering of High-Resolution Triangular Meshes," in *2013 12th International Conference on Document Analysis and Recognition*, Washington, DC, USA, Aug. 2013, pp. 62–66. doi: [10.1109/ICDAR.2013.21](https://doi.org/10.1109/ICDAR.2013.21).

B. Bogacz, M. Gertz, and H. Mara, "Character retrieval of vectorized cuneiform script," in *2015 13th International Conference on Document Analysis and Recognition (ICDAR)*, Tunis, Tunisia, Aug. 2015, pp. 326–330. doi: [10.1109/ICDAR.2015.7333777](https://doi.org/10.1109/ICDAR.2015.7333777).

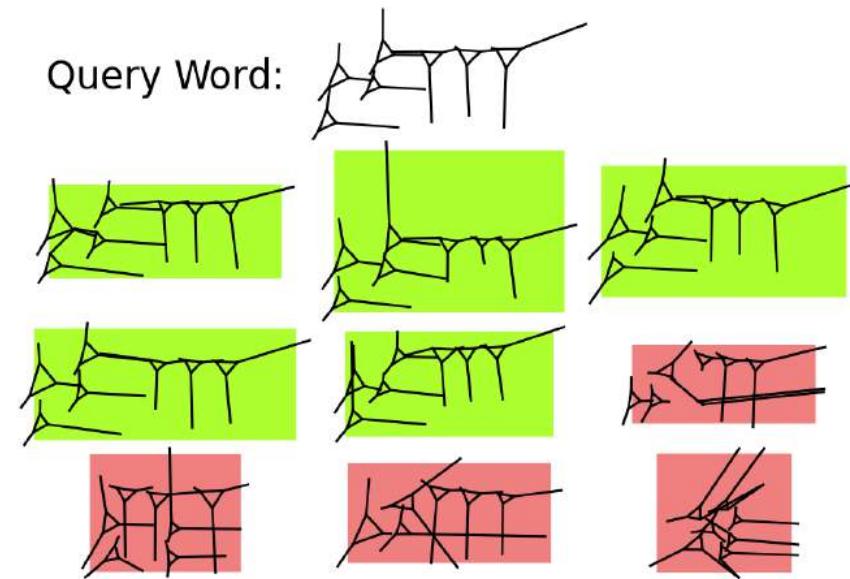
Cuneiform vectorization



Cuneiform recognition

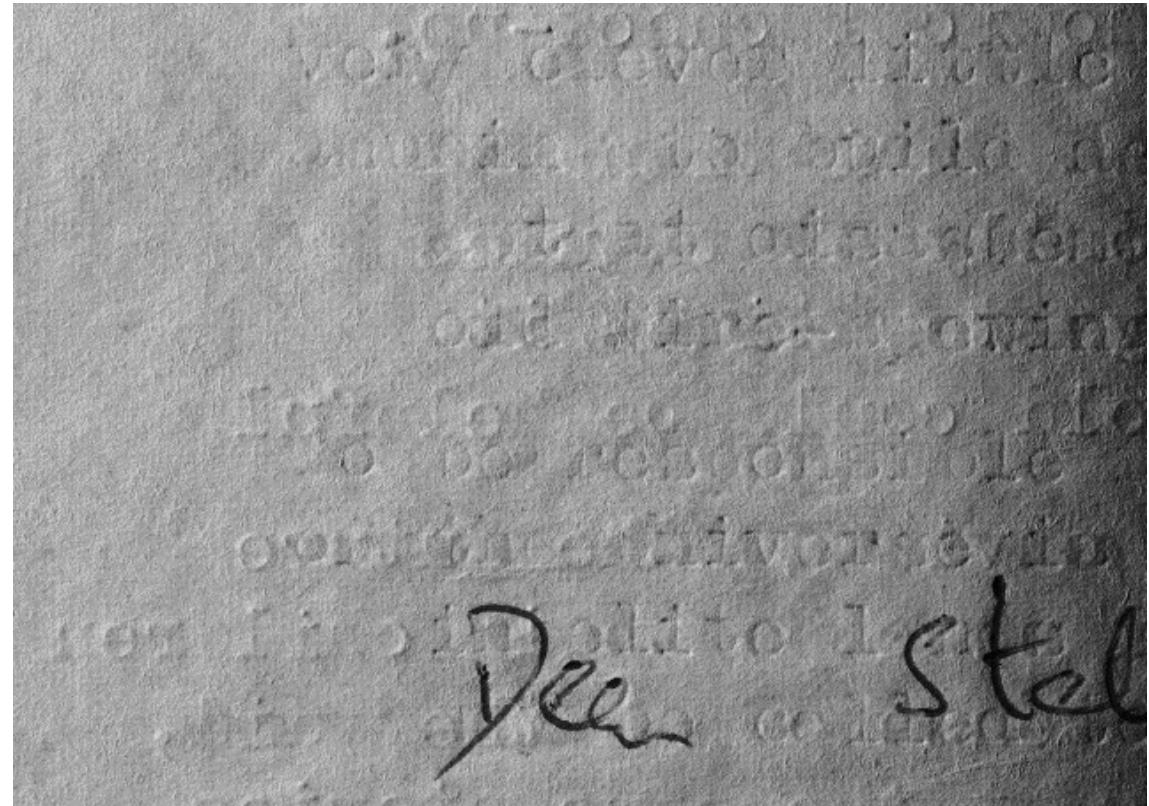


Extraction of structural features



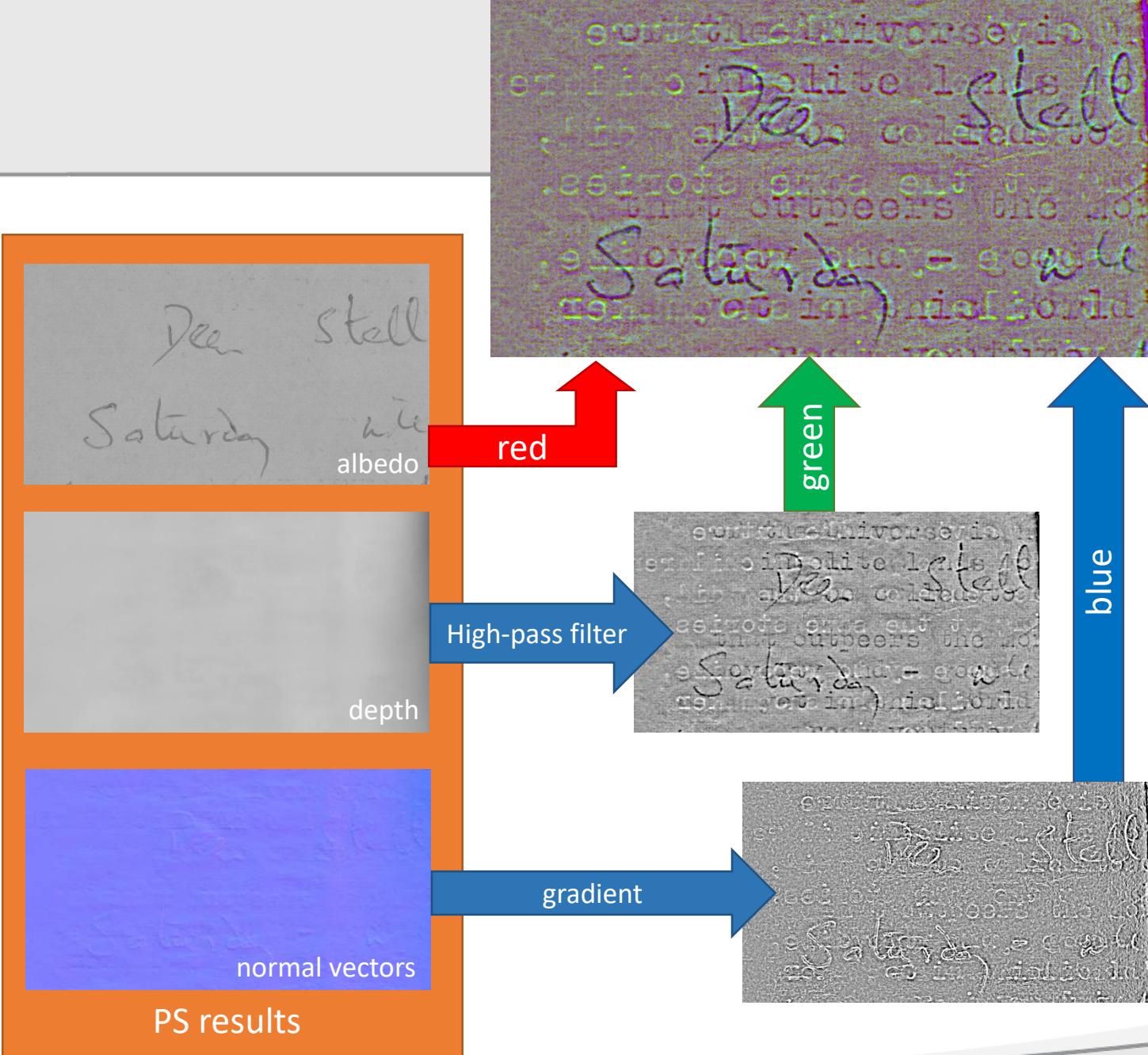
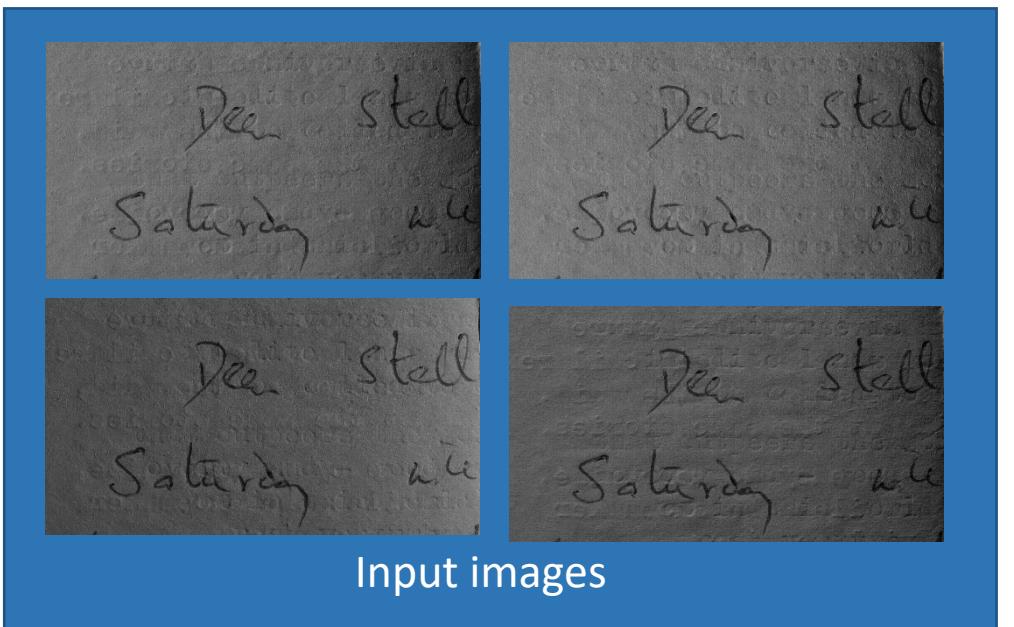
Auden Letters: visualizing typewriter indentations

- Current project: illuminate W.H. Auden's life & work in Australia
- Based on a collection of letters, documents, etc.
- Some of them show indentations from a typewriter
- Our job: make it readable



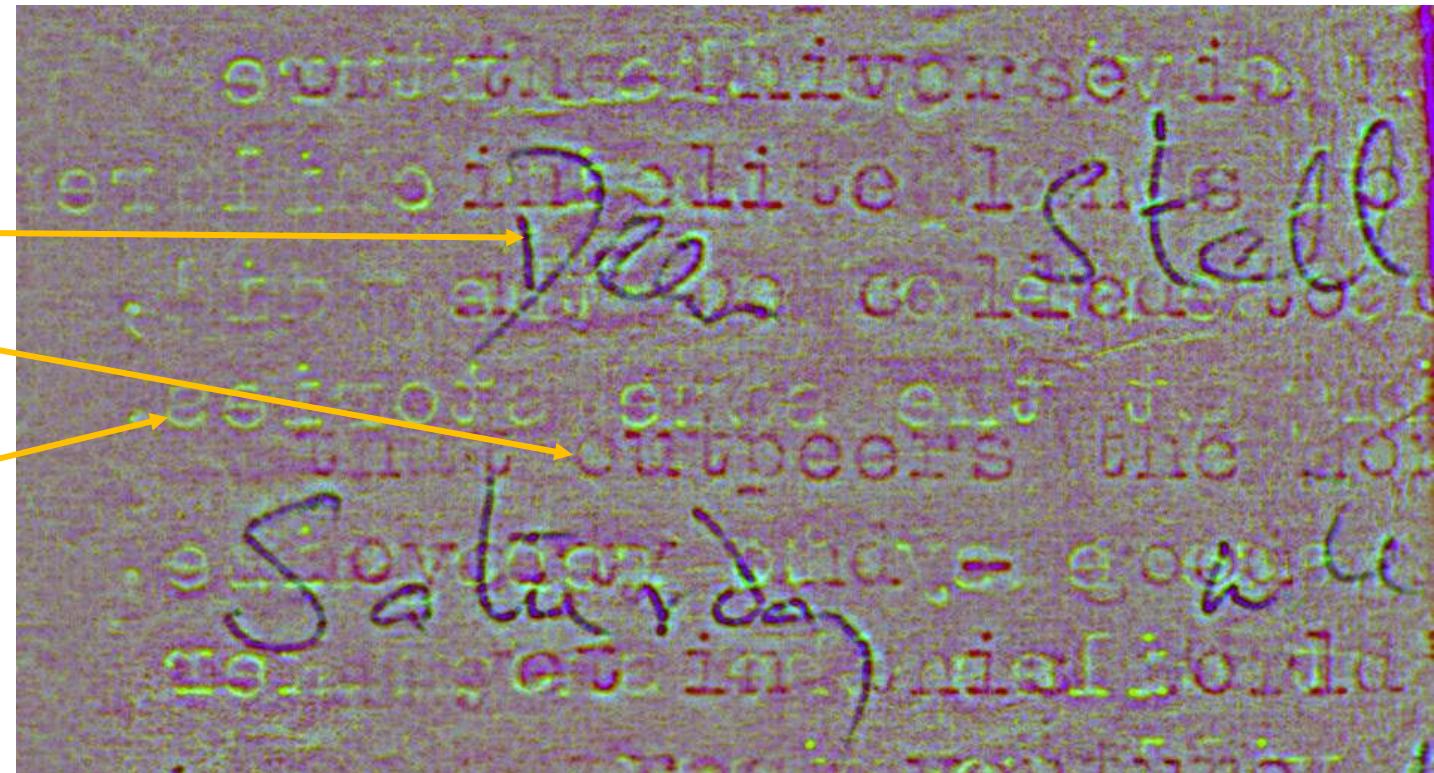
Auden Letters - Approach

1. Photometric stereo reconstruction
2. Filtering
3. Combine results in a false color image



Auden Letters - Results

- Three layers of text
 - Handwritten (black)
 - Impressions from the viewer's direction (red)
 - Impressions from the opposite direction (green)
- An unknown intermediate version of a poem could be identified (and dated)





Computer Vision Lab

Question time